CONSTRUCTION OF THE SUNPATH DIAGRAMS FOR PEKAN AREA FOR SIMULATING THE SOLAR RADIATION EFFECTS TO A BUILDING

# CONSTRUCTION OF THE SUNPATH DIAGRAMS FOR PEKAN AREA FOR SIMULATING THE SOLAR RADIATION EFFECTS TO A BUILDING 

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# Thesis submitted in fulfillment of the requirements for the award of the degree of <br> Bachelor of Mechanical Engineering 

Faculty of Mechanical Engineering UNIVERSITY MALAYSIA PAHANG

## APPROVAL DOCUMENT

## UNIVERSITI MALAYSIA PAHANG CENTER FOR GRADUATE STUDIES

I certify that the thesis entitled " Construction of Sunpath Diagram for Pekan Area for Simulating the Solar Radiation Effects to a Building" is written by Syamimi Soliha binti Mohd. I have examined the final copy of this thesis and in our opinion, it is adequate in terms of languages standard, and report formatting requirement for the award of the degree of Bachelor of Mechanical Engineering. I herewith recommend that it be accepted in fulfillment of the requirements for the degree of Bachelor of Mechanical Engineering.

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I hereby declare that the work in this project is my own except for quotations and summaries which have been properly acknowledged. The project has not been accepted for any degree and is not concurrently submitted for award of another degree.

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Dedicated to my beloved parents, Mohd bin Ibrahim and Ramlah binti Ismail, family, and all my friends
Thank you so much for always being there for me and support me.

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#### Abstract

This thesis deals with the sun is a valuable source that provided to the earth because the sun produce renewable energy and do not pollute the surroundings. However, the sun can create the problem to the population of the earth. Extreme heat produced by the sun radiate directly to the building and may cause lower energy efficiency. This study concentrates on the solar geometry and constructing of sunpath diagram for Pekan Area by simulating the solar radiation that the effect of a building. Pekan, Pahang is taken as my reference location at a latitude $3^{\circ} 29^{\prime}$ North for construct sunpath diagram. There are parameters used for constructing a diagram which is the latitude of the object, declination angle, altitude angle, azimuth angle and hour angle. The sunpath diagram is a way of representing annual changes in the path of the sun through the sky on a single 2D diagram. Based on the sunpath diagram of Pekan Area, shows the altitude angle is highest at the 21st of March in the northern hemisphere, it is also same for September, $21^{\text {st }}$ at southern hemisphere. It is because the sun is directly in line with the equator, it is called as the equinox, where the declination angle for equinox is equal to zero. The equinox occurs when the sun crosses the equator in which day and night are of the same length. Different for in June, $21^{\text {st }}$ and December $21^{\text {st }}$ is a minimum altitude angle at northern and southern hemisphere. The declination angle for both months is the maximum and minimum $23.45^{\circ}$. Summer solstice occurs when northern hemisphere gets more daylight longer than a night, meanwhile winter solstice occurs when southern hemisphere gets more night time rather than daytime. There are many applications for sunpath diagram can be used by architect or engineers. For the example, they can use the sunpath diagram to calculate the solar radiation that radiates the building and how to control. Hence, the sunpath diagram can be used to find the best position for Solar Photovoltaic Cell and Solar Panel, window shading and water solar heating system.


#### Abstract

ABSTRAK

Thesis ini membentangkan tentang matahari mengeluarkan sumber yang berguna kepada bumi kerana matahari mengeluarkan tenaga yng boleh diperbaharui dan tidak mencemarkan keadaan sekeliling. Walau bagaimanapun, matahari juga boleh memberi masalah kepada penduduk di bumi. Haba yang berlebihan yang terhasil daripada matahari boleh memancarkan terus ke bangunan dan menyebabkan kecekapan tenaga yang lebih rendah. Mengambil Pekan sebagai rujukan utama tempat iaitu latitud $3^{\circ} 29^{\prime}$ untuk membentuk kedudukan matahari dari terbit hingga terbenamnya matahari, setiap 21 haribulan dalam satu tahun. Kedudukan matahari ditentukan dengan mengetahui pengetahuan tentang geometri suria dan sudut suria. Ada beberapa asas parameter yang digunakan untuk membentuk kedudukan matahari iaitu latitud sesuatu objek, sudut cerun, sudut ketinggian matahari, sudut azimuth dan sudut jam. Parameter tersebut digunakan untuk membentuk gambar rajah posisi matahari. Berdasarkan gambar rajah kedudukan matahari di Pekan, Pahang menunjukkan sudut ketinggian matahri paling tinggi adalah pada bulan Mac, 21 haribulan dalam hemisfera utara, begitu juga pada bulan September, 21 haribulan dalam hemisfera selatan. Ini kerana, matahari berada di kedudukan sama garis dengan khatulistiwa ataupun ekuinoks dan sudut kecerunannya adalah kosong. Ekuinoks terjadi apabila cahaya matahari sama lurus apabila melintasi khatulistiwa, menyebabkan bumi mengalami kejadian siang malam dalam waktu yang sama lama. Berbeza pula dengan bulan Jun, 21 haribulan dan bulan Disember, 21 haribulan kerana kedua-dua bulan tersebut menunjukkan sudut ketinggian matahri yang paling rendah dalam hemisfera utara dan juga selatan. Sudut kecerunan matahari adalah maksimum $23.45^{\circ}$ dan juga minimum $23.45^{\circ}$. Pada Solstis musim panas, bumi mengalami siang lebih lama kerana hemisfera utara bumi mendapat lebih cahaya matahari manakala pada solstis musim sejuk, hemisfera selatan bumi mengalami malam lebih lama. Terdapat banyak kegunaan gambar rajah kedudukan matahari yang boleh digunakan oleh arkitek mahupun jurutera.Contohnya, mereka menggunakan kedudukan matahari untuk mengira bilangan radiasi yang menembusi bangunan dan cara mengawalnya.Selain itu, mereka mengunakan gambar rajah kedudukan matahari untuk mencari posisi terbaik untuk memasang Tenaga Suria Fotovolta dan Suria Panel, teduhan tingkap dan juga Tenaga Suria sistem pemanas air


## TABLE OF CONTENTS

PAGES
EXAMINER'S DECLARATION ..... ii
SUPERVISOR'S DECLARATION ..... iii
STUDENT'S DECLARATION ..... iv
DEDICATION ..... v
ACKNOWLEDGEMENTS ..... vi
ABSTRACT ..... vii
ABSTRAK ..... viii
TABLE OF CONTENTS ..... ix
LIST OF TABLES ..... xii
LIST OF FIGURES ..... xiii
LIST OF SYMBOLS ..... xiv
LIST OF ABBREVIATIONS ..... xv
CHAPTER 1 INTRODUCTION
1.1 Introduction ..... 1
1.2 Background ..... 1
1.3 Problem statement ..... 3
1.4 Objectives ..... 4
1.5 Scope ..... 4
CHAPTER 2 LITERATURE REVIEW
2.1 Introduction ..... 6
2.2 Energy efficiency ..... 6
2.3 Climate ..... 7
2.4 Solar energy ..... 7
2.5 Solar geometry ..... 8
2.5.1 Rotation ..... 8
2.5.2 Revolution ..... 9
2.5.3 Equinox ..... 10
2.5.4 Solstice ..... 11
2.5.5 Seasons ..... 12
2.6 Sunpath ..... 13
2.6.1 Latitude and longitude ..... 14
2.6.2 Altiude angle and Azimuth angle ..... 14
2.6.3 Declination angle ..... 16
2.6.4 Time ..... 18
2.7 Solar Radiation ..... 18
CHAPTER 3 PROJECT METHODOLOGY
3.1 Introduction ..... 19
3.2 Flow chart ..... 20
3.3 The coding of $\mathrm{C}++$ Programming ..... 21
3.3.1 The equation that will used in $\mathrm{C}++$ programming ..... 21
3.4 Calculate and Tabulate the Data ..... 22
3.5 Method of the Sunpath Diagram ..... 22
3.6 Procedure ..... 22
3.7 Tabulate Data on the Table given ..... 27
CHAPTER 4 RESULTS AND DISCUSSION
4.1 Introduction ..... 32
4.2 Analysis Data for Sunpath Diagram ..... 32
4.2.1 Sunpath Diagram for Pekan Latitude ..... 33
4.2.2 Sunpath Difference for Different Latitude ..... 36
4.3 Application of Sunpath ..... 37
4.3.1 Solar Radiation effects to a building ..... 38
4.3.2 Photovoltaic Cell or Solar Collector ..... 43
4.3.3 Best Installation of Solar Energy ..... 45
CHAPTER 5 CONCLUSION AND RECOMMENDATION
5.1 Introduction ..... 46
5.2 Conclusion ..... 46
5.3 Recommendation ..... 47
REFERENCES ..... 49
APPENDIXES
A ..... 50
B ..... 52
C ..... 70

## LIST OF TABLES

Figure No. Title Page
2.1 Different angle of the sun ..... 9
2.2 Earth's elliptical orbit around the sun ..... 10
2.3 Tilt angle of Equinox plane ..... 11
2.4 Tilt angle of Summer Solstice plane ..... 12
2.5 Tilt angle of Winter Solstice plane ..... 12
2.6 Tilt angle of Solstice plane ..... 12
2.7 Tilt of the earth ..... 13
2.8 Path of the sun in a location ..... 15
2.9 Tropic and northern hemisphere ..... 16
2.10 Variation of declination angle with $n$th day of the year ..... 17
$3.1 \quad$ Coding C++ programming ..... 21
3.2 The hour angle between local solar time in northern hemisphere ..... 24
3.3 Definition of altitude angle and azimuth angle ..... 29
3.4 The hour angle ..... 30
4.1 The sunpath diagram for Pekan area in a year ..... 33
4.2 The sunpath diagram at northern hemisphere ..... 34
$4.3 \quad$ The sunpath diagram at southern hemisphere ..... 35
4.4 The sunpath diagram with different location and angle ..... 36
$4.5 \quad$ Calculation of incident solar angle for vertical surfaces ..... 39
4.6 An arbitrarily oriented surface with tilt angle ..... 40
$4.7 \quad$ Geometry of south facing solar collector ..... 43
$4.8 \quad$ Solar panel at Pekan Campus ..... 44

## LIST OF TABLE

Table No. Title Page3.1 Declination angle for each $21^{\text {st }}$ month of a year25
3.2 Result of 21 ${ }^{\text {st }}$ June 2013 ..... 28
4.1 Locations and Latitudes for three cities ..... 37

## LIST OF SYMBOLS

Altitude angle
Azimuth angle
Declination angle
Direct radiation
Hour angle
Latitude
Incident angle
Surface azimuth angle
Reflectivity
Tilt angle
Total number of days of the year
Total irradiation
View factor
Wall solar azimuth angle
Zenith angle

## LIST OF ABBREVIATIONS

| AST | Apparent Solar Time |
| :--- | :--- |
| DST | Daylight Saving Time |
| FKM | Faculty of Mechanical Engineering |
| GMT | Greenwich Mean Time |
| LST | Local Standard Time |
| UMP | Universiti Malaysia Pahang |
| ST | Solar Time |
| PV | Photovoltaics |

## CHAPTER 1

## INTRODUCTION

### 1.1 INTRODUCTION

The sun is closely related to the earth. It not only provides light to the earth, it gives life to the earth. The sun is the brightest star in the Earth's solar system. And not only does the sun gives us light, but is also a valuable source of heat energy. The sun can be considered as the life giver to living things on this earth, because without the sun, many living thing organism would not exist and survive. However, the sun will also create problems for humans. For example, extreme heat produced by the sun may radiate directly into buildings and may cause lower energy efficiency. The earth rotates every 24 hours, and while it rotates give effect on night a day, it also revolves around the sun making one complete revolution in 365 days. There two movements follow a precise characteristics and geometry called the solar geometry, then giving rise to varying solar radiation which changes gradually. The movement of the sun relative to the earth therefore follows precise paths called sun paths and they can be plotted on a diagram called sun path diagram.

### 1.2 BACKGROUND

The earth rotates about on a fixed plane that is tilted $23.5^{\circ}$ with respect to its orbital plane around the sun. The earth needs 365 days to complete one year per rotation around the sun and the earth also needs 24 hours to complete one true rotation or one day around the sun. It is defined as the time taken for the sun to move from the zenith on one day to the zenith for the next day, or from noon today and to noon tomorrow. Thus, the length of
the solar variability is calculated to be a day or 24 hr . Completing a year, a solar day may differ to as much as approximately 15 min . That is the reason why, for a Muslim, Azan time will be different by a few minutes from day to day and from year to year from Subuh to Isya' prayer's time. There are three reasons for this time difference. Firstly, it is because the earth's motion around the sun is not a perfect circle but it is eccentric. The second reason is due to the fact that the sun's apparent motion is not parallel to the celestial equator. The third reason is because of the precession of the earth's axis. The rotation of the earth also causes the day and night phenomenon. The length of the day and night is depends on the time of the year and the latitude of the location. But for Malaysia, being located close to the equator line, the length of the day and night are almost equal, 12 hours a day and night, but with some variation of about 30 min or so.

The path that the earth takes to revolve around the sun is called the elliptical path. However, to be exact, the number of the days the earth takes to revolve around the sun actually depends on whether referring to a sidereal year or solar year. A sidereal year is the time taken for the earth to complete exactly one orbit around the time interval between two vernal equinoxes. Equinoxes happen when the elliptic in the sun's apparent motion across the celestial sphere and celestial equator intersect. During the equinoxes every point on the earth gets exactly 12 hours of daylight, and 12 hours of night time. The earth is tilted $23.5^{\circ}$ the sun is at a maximum angular distance from the celestial equator. At the summer solstice which occurs around the 21st of June, the North Pole is pointing away towards the sun at a positive angle $23.5^{\circ}$ in the apparent declination of the sun. At winter solstice which occurs around the 21 st of December the North Pole is pointing away towards the sun at a negative angle $23.5^{\circ}$ in the apparent declination of the sun.

Everyone knows that the sun rises in the east and sets in the west. This phenomenon has always amazed the mankind. The sun certainly brings about interest for everyone to study its movement and behavior especially its position at different times of the days and months during the year. The sun will rise and set from a different point of the horizon and move along different paths across the sky. Expect during the equinoxes, the sun does not rise exactly in the east and sets in the west. They are determined by the
latitude of the locality. Measuring the angle of the sun in its motion across the sky is done by measuring altitude and azimuth angles. Altitude angle is the angular distance above the horizon measured perpendicularly to the horizon. The azimuth angle is the angular direction measured along the horizon in a clockwise direction. The sun paths are different due to the factors such as different local or local altitude, rising and setting position which is based on the time of the year and lastly due to the duration of the day and night. The sun path diagram is a way of representing the annual changes in the path of the sun through the sky on a single 2D diagram.

### 1.3 PROBLEM STATEMENT

The energy efficiency of a building is highly dependent on the solar geometry, and therefore the solar geometry must be fully understood for any initiative towards improving the energy efficiency of a building. This is especially true for buildings in a hot climate country like Malaysia, where air-conditioning takes up about 60 to $70 \%$ of the total energy consumed in a building.

The solar geometry has many special effects on the earth. The movements of the earth with respect to the sun create unique characteristics to the earth. The rotation of the earth within the 24 hour period gives rise to day and night, whereas the revolution of the earth around the sun with the earth polar axis inclined at a certain fixed angle gives rise to the changing day and night hours as well as the seasonal changes, from spring to summer to autumn and winter, and back again to summer.

With both movements combined (rotation and revolution) gives rise to further implications to the earth, particularly the solar radiation. The rate of this solar radiation changes every hour of the day, and every day of the year, based on the solar geometry. The solar radiation in turn, gives rise to thermal behavior of a building, and for hot-climatic countries like Malaysia, solar radiation is the major contributor to the air-conditioning load of the building or a space.

Using the knowledge and science of solar-geometry, it is useful to construct Sun path Diagrams for any particular locality. From the sun path diagrams, the engineer and architect can determine the positions of the sun from which the building's orientation can be optimally chosen for the highest energy efficiency, together with the window size and possible use in other applications such as the design of window shade or overhang.

It is not easy to find the Sun path Diagrams ready made for the exact location of the Pekan town. This Final Year Project therefore aims at constructing the Sun path Diagrams for Pekan Town, using a computer program and also data are tabulated in Microsoft Excel Office that will be constructed using the solar geometry equations well established now, to help in the design of energy efficient buildings.

### 1.4 OBJECTIVE

The objectives of this study are:

1. To understand and study of the solar geometry.
2. To construct the sun path diagrams for a Pekan area with a computer programming and also Microsoft Excel Office with the intention of simulating the solar radiation effects to a building.

### 1.5 SCOPE

The purpose of this study is to study the solar geometry and construct the sun path diagram for Pekan area. This requires knowledge of the equations involved that determine the changing position of the sun with respect to the earth.

Based on the equations identified for the solar geometry, a computer program will be constructed and also calculating the data using equation provided. It is expected that the sun path diagram be plotted by the computer using Microsoft Excel Office.

The sun path diagram has its special uses, particularly in constructing horizontal shaded for windows, in determining the best position and angle for constructing photovoltaic panels, and in positioning solar hot water systems. This will be elaborated in the final part of the report.

## CHAPTER 2

## LITERATURE REVIEW

### 2.1 INTRODUCTION

This chapter deals with the review of the solar geometry that would give effect on the earth especially toward energy efficiency in buildings and constructing the sun path diagram for any location or latitude. This chapter begins with a general review of explanations such as a simple definition of the key words and finally constructing the sun path diagrams using knowledge of solar geometry. In this literature review, previous works related to this study are discussed.

### 2.2 ENERGY EFFIENCY

Many engineers try to increase energy efficiency of the building after the building in completely ready. But without realizing it, the solar geometry is one effective initiative for engineers and architects to improve higher energy efficiency level of the building even before construction. Ramly and Hussain (2012) have stated that the main factor of energy efficiency in building design is to create buildings that utilize a minimum amount of energy. Energy efficiency is an important way of reducing carbon emission and possible climate changes as well as to contain the rapid growth of energy consumption in this world, contributing the preventing supply and mitigating the depletion of energy resources as be cited in Santos et al (2012) . The level of energy efficiency for decreasing the total energy consumption is not easily counted or measured. According to Brookes, Herring and Sorrell, increased energy efficiency may increase rather than reduce, energy consumptions. (Santos
et al, 2012). This fact is due to rebound effect caused by reductions in the marginal cost of energy to promote the environments.

The simple definition of energy efficiency considers the relationship between how much the energy is introduced into a process and criteria to be analyzed. Decreasing energy demand at source is not only better in the long term of sustainability, but also in many instances may also endure very little cost (Madomercandy and Haris, 2006). Improving energy efficiency in the building will contribute to the good side of the environment in the future.

### 2.3 CLIMATE

The climate in Malaysia can generally be described as tolerable in terms of thermal requirements. Pereira, Silva and Turkienikz (2001) has stated that the main strategic control for making adequate is passive solar and shading of solar radiation to local climatic condition. The passive solar and shading of solar radiation especially true for buildings in hot climates like Malaysia where air conditioning takes up about $70 \%$ of total energy consumed in a building. Due to Malaysia's orientation located near to the equator plane, Malaysia is a categorized as an equatorial country which being hot and humid throughout a year.

### 2.4 SOLAR ENERGY

The sun is the brightest star in the Earth's solar system. In order to give our earth light, also gives valuable benefits to living things as a source of heat energy. Without the source of energy from the sun, living things in an ecosystem would hardly exist and survive. Since solar energy is a natural resource that does not require burning the fossil fuels and associated with the gas emission, solar energy is considered as renewable energy. Many developing countries have already implemented these energy resources in order to supplement the energy from fossil fuel. Replacing fossil fuels with renewable energy sources can also improve national security by reducing dependence on imported energy,
hence the increasing focus on solar energy devices for their nonpolluting and renewable qualities has led to the recent interest in sustainability and in green buildings (ASHRAE, 2011).

### 2.5 SOLAR GEOMETRY

In the thermal or climatic design of buildings, the sun is the most influential. Understanding of solar geometry is one of the best ways to improving the energy efficiency of the building .Before the engineer or architect come up with the design of the building to control solar energy, it is important to understand the solar geometry and the relationship between sun and earth as the sun will directly affect the thermal behavior of the buildings.

### 2.5.1 ROTATION

The sun has a unique relationship with the earth and gives many special effects to the earth. In a fixed plane tilted at an angle of $23.45^{\circ}$, the earth rotates 24 hours to complete one rotation or sidereal period. The earth's sidereal period will always be 24 hours since the speed of earth's rotation is constant throughout the year. In the course of the year, a solar day may differ to as much as 15 min . For simplicity, the earth completes one rotation every 24 hours based on the solar day and it moves at the rate of $15^{\circ}$ per hrs as full rotation is $360^{\circ}$. Because of the sun appears to move at the rate of $360^{\circ}$ in 24 hours, its apparent rate of motion is 4 min per degree of longitude has been carried out by ASHRAE (2011). The apparent path of the sun's motion across the sky will make the sun produces a daily solar arc at the different latitudes and at the different angles each day. This daily and hourly solar arc is also called the solar path or sun path. The rotation of the earth about its axis also causes the day and night phenomenon. The length of the day and night depends on the time of the year and the latitude of the location.


Figure 2.1 different angles of the sun

Source: Retrieved from<br>http://solarwiki.ucdavis.edu/The_Science_of_Solar/1._Basics/B._Basics_of_the_Sun/VI._T he_Sun's_Motion (2012)

In Figure 2.1 shows that in the northern hemisphere, the shortest solar day occurs around December 21 which is called winter solstice and the longest solar day occurs around June 21 which is the summer solstice. In theory at any time of the equator, the length of the day is equal to the length of the night. In Malaysia, since it is close to the plane, Malaysia equally enjoys almost equal day and night.

### 2.5.2 REVOLUTION

The revolution of the earth around the sun with the earth polar axis inclined at a certain fixed angle gives rise to the changing a day and night hours occur as well as the seasonal changes, from spring to summer to autumn and winter, and it's back again until summer. It is generally that the earth's complete revolution around the sun 365 days. This path that the earth takes to revolve around the sun in one year is called the elliptical path.


Figure 2.2 Earth's Elliptical Orbit around the Sun

Source: Retrieved from The Fall Equinoxes
http://www.srh.noaa.gov/abq/?n=clifeatures_fallequinox (2012)

In Figure 2.2 shows that the earth makes slightly elliptical orbit around the sun in one year per rotation. The elliptical orbit is formed by Earth's elliptical orbit around the sun. As the earth revolves around the sun, the orientation produces varying solar declination. Equatorial plane is tipped $23.45^{\circ}$ from the elliptical plane.

### 2.5.3 EQUINOX

Equinoxes happen when the ecliptic which is the sun's apparent motion across his celestial sphere and celestial equator intersection. The equinoxes are either of the two times when the sun crosses the equator in which day and night are of the same time length. The spring equinox occurs when the sun moves up from below the celestial equator to above it around the $20^{\text {th }}$ of March. The fall equinoxes occur when the sun moves down from upper the celestial equator around the 22 nd of September. The earth experiences 12 hr of a day and a night during the equinoxes and that's how equinoxes get names as equinox mean equal night.


Figure 2.3 Equinoxes

Source: Kothari, D. P. Singal, K. C. and Ranjan, R. "Renewable Energy Source an Emerging Technologies, Reference Book", New Delhi, 2008

Figure 2.3 shows the equinoxes occurs when the sun is directly in line with the equator. Usually, equinoxes happen on March $21^{\text {st }}$ and September $21^{\text {st }}$ when the sun crosses the equator in which day and night are of the same length

### 2.5.4 SOLSTICE

At the summer solstice which occur on $21^{\text {st }}$ June happen when the Northern Hemisphere tip towards the sun at an angle positive $23.45^{\circ}$ with respect to the celestial equator. Meanwhile at the winter solstice occur around $21^{\text {st }}$ December when the Northern Hemisphere tip away from the sun at the angle negative $23.45^{\circ}$ with respect to the celestial equator. During the summer solstice, the sun travelling higher path across the sky meanwhile the sun path is the low sky during the winter solstice. The duration of the day is longer relative to the night when crossing the sky in the summer solstice.


Figure 2.4 Summer Solstice


Figure 2.5 Winter solstice


Figure 2.6 Solstices

Source: Kothari, D. P. Singal, K. C. and Ranjan, R. "Renewable Energy Source an Emerging Technologies, Reference Book", New Delhi, 2008

In Figure 2.4, Figure 2.5 and Figure 2.6 shows that when summer solstice, the Northern Hemisphere tipped toward the sun by $23.45^{\circ}$ and get daylight longer than night time. Meanwhile when in winter solstice, the Northern Hemisphere tipped away from the sun and the duration of night longer than day time.

### 2.5.5 SEASONS

The season is caused by the earth axis which is tilted at $23.45^{\circ}$ with respect to the elliptic due to that fact the axis are always pointed in the same direction. The direction of
the sun was pointed in the northern axis, it will be in winter in the southern hemisphere and summer in the northern hemisphere. The sun's ray reached that part of the surface directly and more concentrated when the northern hemisphere is experiencing summer hence enabling to heat up more quickly. The southern hemisphere receiving an equal amount of light ray at more glancing angle, hence spreading out the light ray therefore is less concentrated and cooler.


Figure 2.7 Tilt of the earth

Source: Retrieved from http://beyondweather.ehe.osu.edu/issue/the-sun-and-earths-climate/the-sun-earth\�\�\�s-primary-energy-source (2012)

The Figure 2.7 shows that the sun's ray reached to the surface of the earth directly, it is caused seasons by earth axis.

### 2.6 SUNPATH

After studying about the knowledge and science of solar geometry, sun path diagram can be constructed at the specific location of orientation. Engineer and architect especially can determine the position of the sun from which the building's latitude from this sun path diagram. Sun path refers to the apparent significant seasonal and hourly positional changes of the sun and length of daylight as the Earth rotates and orbits around the sun.

The sun rises in the east and sets in the west but the uniqueness of this natural phenomenon is the sun is not exactly rises due east and set due west. There are three basic coordinate systems used to predict the solar position such as declination or the positions of celestial object, longitude and latitude of position on the earth and lastly used with time. Hence, affecting the behavior of the sun's lighting and heating characteristic will be effected on the sun path by this latitude and longitude.

### 2.6.1 LATITUDE AND LONGITUDE

Longitude and latitude are familiar geographic coordinates used on the earth. They are a system of polar coordinates. Longitude is measured from the Greenwich meridian, latitude is measured from the equator. Latitude $(\boldsymbol{\ell})$ is the angle subtended by the radial line joining the place in the center of the earth, with the projection of the line on the equatorial plane. Longitude is a geographic coordinate that specifies the east-west position of a point on the Earth's lane. By the longitude and latitude, any position on the Earth's surface can be specified.

### 2.6.2 ALTITUDE ANGLE AND AZIMUTH ANGLE

After explaining the latitude and longitude, the position of the sun can be measured with reference to the horizon. Measuring the angle of the sun in its motion crossing the sky, azimuth and altitude reading need to be taken. Altitude is the angular distance above the horizon measured perpendicular to the horizon. Meanwhile, azimuth is the angular distance measured along the horizon in a clockwise direction. Zenith angle $(\Psi)$ is the vertical angle between the sun's ray and the line perpendicular to the horizontal plane through the point. For azimuth angle, it started exactly from the north at $0^{\circ}$ and increasing clockwise.


Figure 2.8 Path of sun in a location

Source : Retrieved from
http://solarwiki.ucdavis.edu/The_Science_of_Solar/1._Basics/B._Basics_of_the_Sun/VI._T he_Sun's_Motion, (2013)

As in Figure 2.8 show, a schematic of one apparent solar path. From this figure, can define three basic solar angles which are azimuth angle ( $\gamma$ ), zenith angle ( $\Psi$ ) and altitude angle ( $\beta$ ) which are required in the solar radiation.

Because the earth's daily rotation and its annual orbit around the sun are equal, same and predictable, the solar altitude and azimuth can be readily calculated for any data from the time of day when orientation location and declination angle are specified as has been carried out by ASHRAE (2011). Hence, constructing the sun path diagram is to representation on a flat surface of the sun's path across the sky. From this sun path diagram, it is easily and quickly determines the location of the sun at any time of the day and at any time of year because every orientation location has its own sun path diagrams.

### 2.6.3 SOLAR DECLINATION ANGLE

The solar declination ( $\delta$ ) means the earth's tilted axis results in a day by day variation of the angle between the earth-sun line and the earth's equatorial plane (ASHRAE, 2011). The relationship between declination angle and the date from year to year varies to significant degree. The declination angle changes from a maximum value of $+23.45^{\circ}$ on June 21 to a minimum of $-23.45^{\circ}$ on December 22. Meanwhile, the declination will be zero to two equinox days which is March 22 which in fall equinox and September 22 which in the spring equinox. ASHRAE (2001) has stated that with their variation in the distribution of radiation of solar over the earth's surface and the varying number of hours of daylight and darkness, the daily change in the declination is the main reason for the changing the season.


Figure 2.9 Tropic and northern hemisphere.

Source: Kothari, D. P. Singal, K. C. and Ranjan, R. "Renewable Energy Source an Emerging Technologies, Reference Book", New Delhi, 2008

As shows in Figure 2.9 the declination angle is the angle subtended by a line joining the centers of the earth and the sun with its projection on the earth's equatorial plane. Declination occurs as the axis of the earth is inclined to the plane of its orbit at an angle $65^{\circ}$.

The declination may be calculated as suggested by Cooper (1969),

$$
\delta(\text { in degrees })=23.45 \sin \left[\frac{360}{365}(284+n)\right]
$$

Where n is the total number of days counted from fist January till the date of calculation.

For June 21, 2006, $n=31+29+31+30+31+21=173$


Figure 2.10 Variation of declination angle $(\delta)$ with the $n t h$ day of the year

Source: Kothari, D. P. Singal, K. C. and Ranjan, R. "Renewable Energy Source an Emerging Technologies, Reference Book", New Delhi, 2008

### 2.6.4 TIME

In solar work, usually the solar time is used. Solar time is a measured from solar noon which is the time when the sun is appears to across the local meridian. Most the solar work deal only in solar time (ST). Apparent solar time (AST) generally differs from local standard time (LST) or daylight saving time (DST) and difference can be significant, particularly when daylight saving time is in effect. Its apparent rate of motion is 4 min per degree of longitude because the sun appears to move the rate of $360^{\circ}$ in 24 hours.

### 2.7 SOLAR RADIATION

Solar radiation and daylight are essential to life on earth. It is because the sun is radiating considerable energy into the earth. Solar radiation is the energy given off by the sun in all directions and when this energy reaches the earth's surface it will call as insolation. Solar radiation gives out light and heat and approaches the earth as electromagnetic waves. When the direct solar radiation is not blocked by clouds, a combination of bright light and radiant heat or it is experienced as sunshine. When it is blocked by reflecting off another object, it is experienced as diffuse light. The entire living thing on the earth's surface is depending on the absorption of the electromagnetic radiation in the form of heat.

The solar radiation is a major part of building heat gain, to hardness solar energy beneficially it is possible selection of suitable material and landscaping. Thus it is important to be able to understand physic of solar radiation and daylight and particular determine the amount of energy intercepted by the earth's surface. The measuring the solar radiation at every location is not implemented and the engineer has developed empirical equations by utilizing the meteorological data such as number of sun hours, the day length and the number of clear days.

## CHAPTER 3

## METHODOLOGY

### 3.1 INTRODUCTION

This chapter represents and explained the methodology be used in this study and research method reading is conducted. For first stages are to identify the problems and the formulation of research objectives. The research objectives are formulated based on the identified problems. Research scopes are determined through data collection during the literature review of the solar geometry.

A literature review and study has been conducted and used to understand the existing standards such as ASHRAE Handbook and Renewable Energy Resources and Emerging Technologies Reference book to determine the solar geometric characteristics for those related to these standards. Understanding of solar geometry is one of the best ways to improving the energy efficiency of the building.

This study is a practical project assisted by computer simulation. This chapter overviews the approach that will be used in conducting the research. This chapter is divided into 3 sections. There are the concept of solar geometry, the equations that will use in the computer programming and also in Microsoft Excel, and lastly the flowchart.

### 3.2 FLOW CHART



### 3.3 THE CODING OF C++ PROGRAMMING

In computing, C in the letter C is a general purpose programming language. C is one of the most widely used programming languages of all time. Mostly C compiler is available for majority available computer architectures, engineers and operating systems. Hence, $\mathrm{C}++$ programming is used in the declination angle equation.

### 3.3.1 THE EQUATION THAT WILL USED IN C++ PROGRAMMING

There is one of equation used in C++ programming to determine the solar position for any locality at any time of the year and any time of the day.

$$
\delta=23.25 \sin [360 / 365(\mathrm{n}+284)]
$$

Where $n$ is the total number of days counted from first January till the date of calculation. The graph of declination angle can refer to Appendix.

The figure below show the coding for this declination angle,


Figure 3.1 Coding $\mathrm{C}++$ Programming

### 3.4 CALCULATE AND TABULATE THE DATA

There are a number of equations used and calculated using Microsoft Excel. To obtain the result, the equations are used to calculate the azimuth and the altitude angle. After finding the data for latitude, declination angle, and hour angle, so the data for altitude angle were obtained. Then, the azimuth angle can be calculated from the result of the altitude angle.

### 3.5 METHOD OF SUNPATH DIAGRAM

The sunpath diagram is a well known graphic traditionally used by architects and engineers to analyze the position of the sun to improve and control the solar radiation effect to the building. There are many methods of projection that can represent the sun path diagram and in this research, the technique used is an equidistant projection method. The equidistant is becoming a widely used method for constructing a sun path diagram and shading mask protractor in the United States as has been stated by John, Haberl and Degelman (2000). The equidistant method is a method in the projection solar altitude lines are not geometrically but equally spaced as concentric circles on a 2 D diagram. The equation that calculates the altitude angle and azimuth angle as an X and Y coordinate pair used to construct the sunpath diagram. The graph of altitude angle against the azimuth angle can be seen as a result.

### 3.6 PROCEDURE

1. Set up the $N$ as equal to 1 to 365 days. The $N$ is the day of the year (counted from $1^{\text {st }}$ January 2013 ).

$$
N=\text { day of year with } 1^{\text {st }} \text { January }=1
$$

2. Set up the latitude of Pekan as research location. Pekan's latitude is $3^{\circ} 29^{\prime} \mathrm{N}$ with $33^{\circ} \mathrm{C}$ of temperature.
3. The solar declination, $\delta$ will be set up by giving equation. The solar declination, $\delta$ equation is

$$
\text { Declination angle, } \delta=23.45 \sin \left(360 \times \frac{284+N}{365}\right)
$$

For example, the number of days counted is 21 June 2013.

$$
\begin{aligned}
N= & 31+28+31+30+31+21 \\
& =172 \text { days. }
\end{aligned}
$$

For

$$
\begin{aligned}
& \text { Declination angle, } \delta=23.45 \sin \left(360 \times \frac{284+172}{365}\right) \\
& =23.45 \sin \left(449.75^{\circ}\right) \\
& =23.45^{\circ}\left(\text { For June } 21^{\text {st }}\right)
\end{aligned}
$$

Hence, it shows that the axis about which earth rotates is tilted with an angle of $23.45^{\circ}$ to the plane of the earth's orbital plane and the sun's equator. On June $21^{\text {st }}$, summer solstice will occur when the Northern Hemisphere tips toward the sun of maximum tilt angle of $23.45^{\circ}$. Winter solstice happens on December $21^{\text {st }}$ when the Southern Hemisphere tips toward the sun by negative $23.45^{\circ}$.

The calculation of the declination angle above is calculated manually. The declination angle also can be seen also in C++ programming. The coding, the result and the graph of declination angle are shown in the Appendix.
4. The values of $N$ and $\delta$ can be seen in Table 3.1. However, the declination angle can be seen also in C++ programming.
5. Set up the hour angle, $\boldsymbol{h}$ from $0^{\circ}$ to $360^{\circ}$. The hour angle is a measure of the time of the day with respect to solar noon. The hour angle was counted can be seen in Figure 3.1.
6. Define the values of altitude angle, $\beta$ by using this equation

## Altitude angle, $\boldsymbol{\beta}$

$$
=\sin ^{-1}(\cos l \cdot \cos h \cdot \cos d+\sin l \cdot \sin d)
$$

Where:

$$
\begin{aligned}
& \ell=\text { latitude } \\
& \boldsymbol{h}=\text { hour angle } \\
& \boldsymbol{d}=\text { declination angle }
\end{aligned}
$$

An example is shown below for calculating the altitude angle after knowing the declination angle, latitude and hour angle. With the latitude for Pekan being $3^{\circ} 29^{\prime}$, declination angle be taken from previous calculation, and the hour angle is $0^{\circ}$ or $360^{\circ}$.

Altitude angle, $\beta=\sin ^{-1}(\cos l \cdot \cos h \cdot \cos d+\sin l \cdot \sin d)$

$$
\begin{aligned}
& =\sin ^{-1}\left(\cos 3^{\circ} 29^{\prime} \cdot \cos 0^{\circ} \cdot \cos 23.45^{\circ}+\sin 3^{\circ} 29^{\prime} \cdot \sin 23.45^{\circ}\right) \\
& =70.03^{\circ} .
\end{aligned}
$$

7. Define the values of azimuth angle, $\gamma$ by using the equation below. The values of azimuth angle will be

Azimuth angle, $\gamma$

$$
=\cos ^{-1}\left(\frac{\cos l \cdot \sin d-\cos d \cdot \cos h \cdot \sin l}{\cos \beta}\right)
$$

$$
=\sin ^{-1}\left(\frac{\cos d \cdot \sin h}{\cos \beta}\right)
$$

Where:

$$
\begin{aligned}
& \ell=\text { latitude } \\
& \beta=\text { altitude angle } \\
& \boldsymbol{h}=\text { hour angle } \\
& \boldsymbol{d}=\text { declination angle }
\end{aligned}
$$

After getting the result for the altitude angle as shown above, the azimuth angle can be calculated as shown by the example below:

Azimuth angle, $\gamma$

$$
\begin{gathered}
=\cos ^{-1}\left(\frac{\cos l \cdot \sin d-\cos d \cdot \cos h \cdot \sin l}{\cos \beta}\right) \\
=\sin ^{-1}\left(\frac{\cos d \cdot \sin h}{\cos \beta}\right) \\
=\sin ^{-1}\left(\frac{\cos 23.45^{\circ} \times \sin 0^{\circ}}{\cos 70.033^{\circ}}\right)
\end{gathered}
$$

$$
=0^{\circ} .
$$

The result is tabulated in Table 4.1. However, the full results were calculated for all the months in a year as shown in Appendix.


Figure 3.2 : This diagram depicts the relationship between the hour angle and local solar time in the Northern Hemisphere.

Source: Retrieved from Sustainable by Design: Hour Angle http://www.susdesign.com/popups/sunangle/hour-angle.php (2013)

Figure 3.1 shows that the hour angle at a specific hour of a day throughout the year on the position of the sun. Solar noon is a point when the sun is at its highest in the sky and can be appear to be due the North or the South. Hour angle is equal to positive angle forenoon, meanwhile hour angle is negative at evening.

### 3.7 TABULATE DATA ON THE TABLE GIVEN.

The table 3.1 below show the declination angle calculating with number a day of the year using the equation was given at procedure. For this research, the equation of time for the $21^{\text {st }}$ day of each month of the year was being calculated.

| MONTHS | DAY OF YEAR, $N$ | DECLINATION ANGLE, $\delta$ |
| :---: | :---: | :---: |
| 21 JANUARY | 21 | $-20.16^{\circ}$ |
| 21 FEBRUARY | 52 | $-11.24^{\circ}$ |
| 21 MARCH | 80 | $-0.40^{\circ}$ |
| 21 APRIL | 111 | $11.59^{\circ}$ |
| 21 MAY | 141 | $20.16^{\circ}$ |
| 21 JUNE | 172 | $23.45^{\circ}$ |
| 21 JULY | 202 | $20.46^{\circ}$ |
| 21 AUGUST | 233 | $11.76^{\circ}$ |
| 21 SEPTEMBER | 264 | $-0.20^{\circ}$ |
| 21 OCTOBER | 294 | $-11.76^{\circ}$ |
| 21 NOVEMBER | 325 | $-20.46^{\circ}$ |
| 21 DECEMBER | 355 | $-23.45^{\circ}$ |

Table 3.1: The result of Declination angle, $\delta$ for each $21^{\text {st }}$ months per years
DATE : 21 JUNE $2013 \quad(+\mathrm{VE})$
$\delta=\left(23.45^{\circ}\right)$
$\mathrm{L}=3^{\circ} 29^{\prime}$

| HOUR ANGLE, $\boldsymbol{h}$ | AZIMUTH ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE ANGLE, $\beta$ |
| :---: | :---: | :---: |
| -90 | -66.569 | 1.385 |
| -80 | -66.763 | 10.555 |
| -70 | -66.294 | 19.715 |
| -60 | -65.05 | 28.815 |
| -50 | -62.762 | 37.786 |
| -40 | -58.959 | 46.516 |
| -30 | -52.709 | 54.796 |
| -20 | -42.268 | 62.197 |
| -10 | -24.932 | 67.799 |
| 0 | 0 | 70.033 |
| 10 | 24.932 | 67.799 |
| 20 | 42.268 | 62.197 |
| 30 | 52.709 | 54.796 |
| 40 | 58.959 | 46.516 |
| 50 | 62.762 | 37.786 |
| 60 | 65.05 | 28.815 |
| 70 | 66.294 | 19.715 |
| 80 | 66.763 | 10.555 |
| 90 | 66.569 | 1.385 |
| 0 |  |  |
| 10 |  |  |

Table 3.2 Result for $21^{\text {st }}$ of June 2013

An example in Table 3.2 above was shown the data will calculate to represent the sun path diagram by using the equation azimuth angle and altitude angle. An example table starting day $21^{\text {st }}$ January 2013 with counted number a day of the year and declination angle
for this calculation. For hour angle, it's starting with $90^{\circ}$ with respect to solar noon. The solar noon occurs when the sun at the highest point in the sky and it is symmetric to hour angle. The hour angle is $0^{\circ}$ at solar noon and varies from $0^{\circ}$ to $360^{\circ}$ to complete one rotation since the sun takes 24 hours for one rotation. The equation of time for hour angle being positive in the afternoon and negative in the forenoon.

For January $21^{\text {st }}$, the sun path diagram will be plotted on negative graph or in the southern hemisphere. These cases an be same for another month such as February $21^{\text {st }}$, September $21^{\text {st }}$, October $21^{\text {st }}$, November $21^{\text {st }}$ and also December $21^{\text {st }}$. This occurs due to southern hemisphere tip toward the sun and negative solar declination at equatorial plane.

For the next example on March $21^{\text {st }}$, the sun path diagram will be plotted on positive graph or in the northern hemisphere. These cases an be same for another month such as April $21^{\text {st }}$, May $21^{\text {st }}$, June $21^{\text {st }}$, July $21^{\text {st }}$ and also August $21^{\text {st }}$. This occurs due to northern hemisphere tip toward the sun and positive solar declination at equatorial plane.


Figure 3.3 Definition of altitude angle and solar azimuth angle.

Source : Kharagpur, IIT. Cooling and Heating Load Calculations -Estimation of Solar Radiation (2010)

This figure shows the altitude angle, $\beta$ is maximum at solar noon. Since the hour angle, at solar noon is equal to $0^{\circ}$.

### 4.1.4 HOUR ANGLE EQUATION

The hour angle represents the position of the sun at a specific hour of the day throughout the year. The hour angle is paired with the declination to fully indicate the direction of a point on the celestial sphere in the equatorial coordinate system. The $360^{\circ}$ circumference of the earth, in term of time, represents 24 hours. One hour is equal $15^{\circ}$ longitude, or 4 minutes equal $1^{\circ}$ longitude. Hence, a reference longitude of saying, $90^{\circ}$ is 6 hours ahead as referring to Greenwich Mean Time (GMT). In solar angle perspective, at solar noon the hour angle is $0^{\circ}$, with the time before solar noon expressed as negative degrees, and the local time after solar noon expressed as positive degrees. Thus, the daily time mentioned in sun path diagrams refer strictly to solar time.


Figure 3.4 The hour angle Source : Retrieved from The Sun's Position, http://www.powerfromthesun.net/Book/chapter03/chapter03.html (2013)

Figure 3.4 shows the hour angle, defined as the angle between the meridian parallel to the sun rays and the meridian containing the observer.

### 4.1.5 SOLAR TIME

Solar time was based on the 24 hour clock with 12:00 at the time that the sun exactly lie on the North-South plane. Because of latitude, longitude and reference time zones, solar time does not equate directly with the local clock time of each time. The hour angle is calculated based on local solar time. Since the earth's orbital velocity varies throughout the year, the local solar time as measured by a sundial varies slightly from the mean time kept by a clock running at a uniform rate.

## CHAPTER 4

## RESULT AND DISCUSSION

### 4.1 INTRODUCTION

A convenient way of representing the annual changes in the path of the sun through the sky using 2D diagrams is Sunpath Diagram. Thus, to get the full diagram position of the sun after knowing the latitude of the specific coordinates is by calculating, the declination angle using solar declination equations and then calculating the altitude angle. The angle of the sun in its motion is measured by using the equation of altitude angle and azimuth angle. But for declination angle, the data were determined by using C++ programming. The coding of the programming is included in the Appendix. After getting the result for these both equations, the graph of altitude angle against azimuth angle for the sunpath diagram is plotted using the Microsoft Excel. Refer to the Appendix for the result obtained from the equations. The sunpath diagram is a vertical version of the equidistant representation, where the horizontal lines of latitude are equally spaced.

### 4.2 ANALYSIS OF DATA FOR SUNPATH DIAGRAM

The result of the calculations obtained as shown in Table 4.1. The position of the sun at any time of the day of month of the year can be directly read from the diagram in Figure 4.2.1 and Figure 4.2.2. This figure shows the azimuth angle plotted along the horizontal X axis while the altitude is plotted vertically along the Y axis.
4.2.1 SUN PATH DIAGRAM FOR PEKAN LATITUDE


Figure 4.1 Sunpath Diagram for each month of the year.


Figure 4.2 At Northern Hemisphere

Figure 4.2 shows the sunpath diagram which basically depicts the latitude angle against azimuth angle or sunpath diagram. Pekan, Pahang is taken as my reference location at a latitude for $3^{\circ} 29^{\prime}$ North Latitude. In the Northern Hemisphere, it is noted that the sun path a solar azimuth angle range of $0^{\circ}$ to $360^{\circ}$. Referring to Table 1.1 , the hour angle took from $0^{\circ}$ until $90^{\circ}$ due east and $270^{\circ}$ to $360^{\circ}$ due west. It shows that 21 March gives maximum altitude angle because the declination angle for 21 March is equal to $0^{\circ}$, meanwhile 21 June gives minimum altitude angle due to declination angle is exactly maximum positive $23.47^{\circ}$. On 21 March, the sun is directly overhead the equator, known as equinox (a day of equal nighttime and daytime hours). For 21 April and 21 August, the sun chart is nearly the same for both because of the declination angle for both months is nearly same which is $11.59^{\circ}$ and $11.76^{\circ}$. Hence, for both 21 May and 21 July, they also
have nearly same the path due to declination angle for both months is the same which is $20.16^{\circ}$ and $20.46^{\circ}$


Figure 4.3 At Southern Hemisphere

Figure 4.3 shows the sunpath for Pekan, Pahang which is again taken as the reference location with a latitude of $3^{\circ} 29^{\prime}$ North Latitude. In the Southern Hemisphere, it is noted that the sun chart has a solar azimuth angle range of $0^{\circ}$ to $360^{\circ}$. Refer to Table 4.2 in Appendix, where the hour angle is taken from $90^{\circ}$ until $270^{\circ}$ due east and due west. It shows that 21 September results in a maximum altitude angle due to declination angle for 21 September which is equal to $0^{\circ}$. Meanwhile 21 December results in a minimum altitude angle due to declination angle of exactly maximum negative $23.47^{\circ}$. On 21 September, the
sun is directly overhead at the equator, known as equinox (a day of equal nighttime and daytime hours). For 21 October and 21 February, the sun chart is nearly the same for both because of the declination angle for both months is almost equal which is $-11.24^{\circ}$ and $11.76^{\circ}$. Hence, for 21 November and 21 January, the sun chart is almost equal because the declination for both months is $-20.46^{\circ}$ and $-20.16^{\circ}$.

### 4.2.2 SUNPATH DIFFERENCE FOR DIFFERENT LATITUDES

Different latitude and different day of the year, will the result in different path of the motion of the sun, different times of sunrise and sunset, and the duration of the sun above the horizon. As shown in Figure 4.2, the sun is not necessarily rising due east or due west, nor exactly in equator plane.


Figure 4.4 Sunpath Diagram

Source: GEK 1506 Heavenly Mathematics - Sun and Architure (2006)

Figure 4.4 shows the position of the sun depending on the day of the year and the latitude of the observer. It determines where the sun rises and sets or how long the sun is above the horizon.

| Location | Latitude |
| :--- | :--- |
| Johor Bharu | $1^{\circ} 28^{\prime}$ |
| Pekan | $3^{\circ} 29^{\prime}$ |
| Kuala Perlis | $6^{\circ} 25^{\prime}$ |

Table 4.1 Locations and latitudes

The latitude can be described as the angular difference away from the equator. As a reference, the latitude of the equator is 0 degrees. To show the difference of latitude with the respect to sun path diagrams three cities which is Johor Bharu, Pekan and Kuala Perlis are chosen. There are three cities are chosen because Johor Bharu is located at the lowest latitude in Peninsular Malaysia, whereas Kuala Perlis is located at the highest latitude at the Peninsular Malaysia. Pekan is of course earlier taken as the main study of this project, and located almost in the middle of the two latitudes.

The altitude of sunpath for Kuala Perlis is a minimum angle rather than the altitude angle for Pekan and Johor Bharu. For the sunpath for Johor Bharu and Kuala Perlis, please refer to the Appendix. The latitude of Johor Bharu is near to 0 degrees which is near to the equator, so the altitude is maximum angle is $88.128^{\circ}$. For the equator, altitude angle is exactly $90^{\circ}$. So, it shows that the difference in angles between Johor Bharu and the equator is small.

### 4.3 APPLICATION OF THE SUNPATH DIAGRAM

Malaysia is a South- East Asian country which is situated in a tropical region and near to the equator. Geographically, it consists of two distinct regions embracing Peninsular Malaysia to the west and East Malaysia to the east, which is separated by the South China Sea. The country lies between $1^{\circ}$ and $7^{\circ}$ North Latitude, with hot and humid climate and heavy tropical rains. As place of the subject, Pekan is $3^{\circ} 29^{\prime} \mathrm{N}$, longitude $103^{\circ}$ $22^{\prime} 04^{\prime \prime} \mathrm{E}$ with $33^{\circ} \mathrm{C}$ of temperature. Pekan experiences constant high temperature and
relative humidity, light and variable wind conditions, long hours of sunshine with heavy rainfall and overcast cloud through the year.

Countries in the tropics do not want excessive heating from the sun while in higher latitude countries welcome the sun's warmth during the winter months. Hence, the amount of heating required depends largely on the latitude and the function of the building. The orientation of the building used in the design plays an important role in controlling the sun's heat.

### 4.3.1 SOLAR RADIATION EFFECT TO A BUILDING

In designing the buildings and structures, architects and engineers have constantly focused their attention towards the sun. The sun produces the energy that can be used to complement to light in the interior facades and rooms, on the other hand incorporated properly into the design of the building. Hence, designing the building is not only to collect energy from the sun which is providing heat and light as in the case for countries experiencing winter, in the case of countries located near the equator but also to reject the solar energy when is can lead to overheating of the building.

Applying the sun path diagram can reduce the energy efficiency toward the building and can control solar radiation that radiates to the building. At the same time, this will reduce the fossil fuel consumptions of buildings as well as results in building that acts in conjunction with natural forces and not against it. Knowing the knowledge of the sun and the sun's path, the building can be designed to fully utilize the available solar energy.

The calculate below shows an example equation used for solar radiation calculations from various solar energy applications.


Figure 4.5 Calculation of incident solar angle for vertical surfaces

Source : Kharagpur, IIT. Cooling and Heating Load Calculations -Estimation of Solar Radiation (2010)

The surface azimuth angle, is the angle between the normal to the wall and south. When the wall facing south, the surface azimuth angle is zero and when it faces west, then surface azimuth angle is $90^{\circ}$.

The wall solar azimuth angle, $\alpha$ is the angle between normal to the wall and the projection of sun's rays on to a horizontal plane.

The arbitrarily oriented surfaces, $\Theta$ is for any surface that is tilted at an angle $\Sigma$ from the horizontal as shown in Figure 4.8. For example, for horizontal surface, $\Sigma$ is $0^{\circ}$, hence $\Theta$ is equal to $(90-8)$. Similarly for vertical surface, $\Sigma$ is $90^{\circ}$, hence $\theta$ is equal to $\cos ^{-1}(\cos \beta \cdot \cos \alpha)$.


Figure 4.6 An arbitrarily oriented surface with a tilt angle $\Sigma$
a) Example: Calculate the angle of incidence at 2 P.M (solar time) of a north- facing roof that is tilted at an angle of $15^{\circ}$ with the respect to the horizontal. Location at Pekan and date is $21^{\text {st }}$ September.

Given: Latitude,$=3^{\circ}{ }^{\circ} 9^{\prime}$
Solar time $=2$ P.M $=$ hour angle, $\boldsymbol{h}=30^{\circ}$
Tilt angle, $\Sigma=15^{\circ}$
Date $=21^{\text {st }}$ of September 2013
Declination angle, $\delta=\left(-0.20^{\circ}\right)$

Since the roof is north facing, the surface azimuth angle, is equal to $180^{\circ}$ Refer to the Figure 4.3 and Table at appendix, the altitude angle at $21^{\text {st }}$ September is $59.841^{\circ}$. The azimuth angle at $21^{\text {st }}$ September is $84.392^{\circ}$.

The wall solar azimuth angle, $\alpha=180-(\gamma+\xi)=180-\left(84.392^{\circ}+180^{\circ}\right)$

$$
=275.61^{\circ} .
$$

Hence, the angle of incidence is

$$
\begin{aligned}
\Theta & =\cos ^{-1}(\sin \beta \cdot \cos \Sigma+\cos \beta \cdot \cos \alpha \cdot \sin \Sigma) \\
& =\cos ^{-1}\left(\sin 59.841^{\circ} \cdot \cos 15^{\circ}-\cos 59.841^{\circ} \cdot \cos 275.61^{\circ} \cdot \sin 15^{\circ}\right) \\
& =34.66^{\circ} .
\end{aligned}
$$

This equation si general equation and can be used for any arbitrarily oriented surface.
b) To find the direct normal radiation on June $21^{\text {st }}$ at Pekan at solar noon.From the table at appendix, on June $21^{\text {st }}$ at solar noon, the altitude angle for Pekan is $70.013^{\circ}$.

$$
\begin{aligned}
& I_{D N}=A \cdot \exp (-B / \sin \beta) \\
& \quad=1080 \cdot \exp (-0.21 / \sin 70.013) \\
& =863.73 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

where A is the apparent solar irradiation which is taken as $1230 \mathrm{~W} / \mathrm{m}^{2}$ for the months of December and January and $1080 \mathrm{~W} / \mathrm{m}^{2}$ for mid summer. Constant B is called as atmospheric extinction coefficient, which takes a value of 0.14 in winter and 0.21 in summer.
c) To find the diffuse and total solar radiation incident on a horizontal surface located at Pekan on June $21^{\text {st }}$ at solar noon.

From the previous example, on June $21^{\text {st }}$ the direct solar radiation is equal to 863.73 $\mathrm{W} / \mathrm{m}^{2}$. Since the surface is horizontal, the view factor for diffuse radiation, $\mathrm{F}_{\mathrm{ws}}$ is equal to 1 , whereas it is for reflected radiation. Hence, the diffuse solar radiation is given by:

$$
\begin{aligned}
I_{d} & =\mathrm{C} \cdot I_{D N} \cdot F_{w s} \\
& =(0.135 \times 863.73 \times 1) \\
& =117.6 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

The value of C is assumed to be constant for a cluodness sky for an average monthly values. The value of C is 0135 for mid summer and 0.058 for winter. Meanwhile, $F_{w s}$ is called as view factor or configuration factor and is eequal to the fraction of the diffuse radiation that is incident on the surface. Since, the surface is horizontal, the reflected solar radiation is zero. The angle of incidence is given:

$$
\begin{aligned}
\theta & =(90-8) \\
& =(90-70.013) \\
& =19.987^{\circ} .
\end{aligned}
$$

Hence, the total incident solar radiation:

$$
\begin{aligned}
\mathrm{I}_{\mathrm{t}} & =I_{D N} \cdot \cos \mathrm{\theta}+I_{d} \\
& =(863.73 \times \cos 19.987+117.6) \\
& =929.31 \mathrm{~W} / \mathrm{m}^{2} .
\end{aligned}
$$

### 4.3.2 PHOTOVOLTAIC CELL OR SOLAR COLLECTOR

Solar energy can be utilized directly through a variety of devices such as photovoltaic (PV) cell or solar collector. Photovoltaic Solar Panel are means of converting
sunlight directly into electricity via the usage of solar cells. into a flow of electrons. Solar photovoltaics are a sustainable energy source. After hydro and wind power, solar photovoltaics are a third most important renewable energy source in terms of global installed capacity. Solar cells produce direct current electricity from sunlight which can be used to power equipment to recharge a battery. This heat that has been created using these solar thermal collectors is then deployed for use in warm up fluids. In turn, these warming up produce the steam that is used to running turbine in order to generate electricity.

Installing the proper solar collector need to consider the amount of radiation flux incident upon the collector. Actually, the amount of radiation flux upon a solar collector is mainly affected by installation angle, $\beta$. The proper design of the installation of the collector can increase the irradiation received as shown in Figure 4.12 below.


Figure 4.7 Geometry of south-facing solar collector

Source: Chang (2009)

The tilt angle angle varies with factors such as the geographic latitude, climate condition, and utilization period of time.

From the journals reviewed earlier, Chang (2009) has stated that, the optimal orientation is due to the south in the northern hemisphere. The performances of a solar
collector are highly influenced by its orientation and its angle of tilt with the horizontal. The optimum tilt angle varies according to the latitude and the days of the year. As can seen from Figure 4.4, sunpath diagram of Pekan Area, on September and March is highest altitude angle and approximately equal to the latitude. Gunerhan and Hepbasli (2005) have stated that a solar collector tilted angle at an angle equal to the latitude will receive solar radiation nearly normal for these months.

The Figures below show a solar panel installed in the UMP Campus Pekan area. This picture was taken in June, 2013 at 10.30 a.m. This solar panel's latitude is $30^{\circ}$ east of south. The solar panel was facing toward the south in the northern hemisphere. However, the inclined plane for this solar panel is around $15^{\circ}$.


Figure 4.8 Solar Panel at Pekan Campus

Actually, from the assessment, photovoltaic cell or solar collector's best declination is almost to zero or flat surface by toward the south. This is because Pekan is close to equator, and the ideal position for a solar panel along. The equator is flat or zero inclination $(\beta=0)$. However, for pratical reasons, it is good to avoid the solar panel being installed horizontally, as it will collect more dust and dirt during the no rain periods, whereas when it rains the panel will be subjected to vertical impact of the rainwater falling.

### 4.3.3 BEST INSTALLATION OF SOLAR ENERGY

Solar energy is non-polluting, clean, reliable and renewable energy source of electricity. It does not pollute the air through releasing of harmful gases like carbon dioxide, nitrogen oxide and sulfur oxide. In PV cell, usually it is installed on the ground or on the flat surface. Along the equator the best position for PV cell is horizontally rather than south facing, but to avoid the panel collecting dirt and dust, it must be slightly tilted and the most optimum tilting is a few degrees to the south. For Pekan's latitude, following the same rationale as mentioned in the previous section, it is best to install the panel with few degrees facing south. Installing the solar system would contribute to the green generation of electricity. If the roof of the house is surrounded by trees, it is not suitable enough to install the solar panel or solar water heater to produce solar power. Landscapes or other building may be problematic because the shadows can prevent the solar energy to directly reflect to the panels. Climatic condition also needs to take consider when installing the solar systems. Areas which remain mostly cloudy and foggy or rainy season will still produce electricity but in little rate and may require more panels to generate enough electricity. For example, if the sky is cloudy for two days, the solar water heater still produces warm water as the water get heated due to diffused radiation

## CHAPTER 5

## CONCLUSION AND RECOMMENDATION

### 5.1 INTRODUCTION

The sunpath diagram of Pekan town is successfully being plotted by using the results provided by the equations introduced in earlier chapters using the Microsoft Excel subsequently the result of the twelve months in a year were obtained. The sunpath diagram is a way representing annual changes in the path of the sun through the sky on a single 2 D diagram.

### 5.2 CONCLUSION

The sunpath can be determined by the knowledge about solar geometry and solar angle. The altitude angle is highest at the 21st of March in the northern hemisphere, it is also same for September, $21^{\text {st }}$ at southern hemisphere. It is because the sun is directly in line with the equator, it is called as the equinox, where the declination angle for equinox is equal to zero. The equinox occurs when the sun crosses the equator in which day and night are of the same length. Different for in June, $21^{\text {st }}$ and December $21^{\text {st }}$ is a minimum altitude angle at northern and southern hemisphere. The declination angle for both months is the maximum and minimum $23.45^{\circ}$. Summer solstice occurs when northern hemisphere gets more daylight longer than a night, meanwhile winter solstice occurs when southern hemisphere gets more night time rather than daytime

By constructing the sunpath diagram, many applications can be used by engineers and architects. Therefore, the building can be created and designed optimising solar energy as a source of renewable energy, at the same time helps reducing environmental problems of both globally and locally.

### 5.3 RECOMMENDATION

This project has focused particularly on the Pekan latitude, which is $3^{\circ} 29^{\prime}$ North. Different latitudes will be characterized by different sunpath diagrams. For other cities and towns in Malaysia , therefore their own sunpath diagrams need to be constructed to conduct the above exercise with accuracy. The sunpath diagram can be applied:

1. To determine the best position and angle of inclination for Photovoltaic panels, solar hot water systems, solar panel system and also for window shading.
2. To analyze the thermal behavior of a building and can $b$ used to design the Green Building which will reduced the pollution and save our environment.
3. To calculate the radiation directly entering into a building and determine the energy efficiency in the building.

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## APPENDIX A

## C++ PROGRAMMING FOR DECLINATION ANGLE

For example,

For April 8, 2013,

$$
\begin{aligned}
n & =31+29+31+8 \\
& =100
\end{aligned}
$$

The coding:


## Run:



The graph of declination angle :


## APPENDIX B

DATE: 21 JANUARY 2013

$$
\mathrm{N}=\left(-20.16^{\circ}\right) \quad \mathrm{L}=3^{\circ} 29^{\prime}(\mathrm{PEKAN})
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 69.874 | -1.2 | 180 | 0 | -73.323 |
| 100 | 70.13 | -10.582 | 190 | -29.524 | -70.683 |
| 110 | 69.803 | -19.963 | 200 | -47.87 | -64.347 |
| 120 | 68.791 | -29.304 | 210 | -57.885 | -56.347 |
| 130 | 66.859 | -38.553 | 220 | -63.541 | -47.623 |
| 140 | 63.541 | -47.623 | 230 | -66.859 | -38.553 |
| 150 | 57.885 | -56.347 | 240 | -68.791 | -29.304 |
| 160 | 47.87 | -64.347 | 250 | -69.803 | -19.963 |
| 170 | 29.524 | -70.683 | 260 | -70.13 | -10.582 |
| 180 | 0 | -73.323 | 270 | -69.874 | -1.2 |

DATE: 21 FEBRUARY 2013

$$
\begin{gathered}
\mathrm{N}=\left(-11.24^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 78.78 | -0.679 | 180 | 0 | -82.243 |
| 100 | 79.202 | -10.477 | 190 | -51.42 | -77.416 |
| 110 | 79.299 | -20.285 | 200 | -67.56 | -68.719 |
| 120 | 79.022 | -30.089 | 210 | -73.751 | -59.282 |
| 130 | 78.254 | -39.877 | 220 | -76.712 | -49.624 |
| 140 | 76.712 | -49.624 | 230 | -78.254 | -39.977 |
| 150 | 73.751 | -59.282 | 240 | -79.022 | -30.089 |
| 160 | 67.56 | -68.719 | 250 | -79.299 | -20.285 |
| 170 | 51.42 | -77.416 | 260 | -79.202 | -10.477 |
| 180 | 0 | -82.243 | 270 | -78.78 | -0.679 |

DATE: 21 MARCH 2013

$$
\begin{gathered}
\mathrm{N}=\left(-0.40^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -89.601 | -0.024 | 360 | 0 | 86.117 |
| 280 | -88.977 | 9.956 | 10 | 68.963 | 79.278 |
| 290 | -88.307 | 19.935 | 20 | 79.385 | 69.637 |
| 300 | -87.53 | 29.91 | 30 | 83.197 | 59.766 |
| 310 | -86.556 | 39.878 | 40 | 85.246 | 49.835 |
| 320 | -85.246 | 49.835 | 50 | 86.556 | 39.878 |
| 330 | -83.197 | 59.766 | 60 | 87.53 | 29.91 |
| 340 | -79.385 | 69.637 | 70 | 88.307 | 19.935 |
| 350 | -68.963 | 79.278 | 80 | 88.977 | 9.956 |
| 360 | 0 | 86.117 | 90 | 89.601 | -0.024 |

DATE: 21 APRIL 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.59^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.431 | 0.699 | 360 | 0 | 81.893 |
| 280 | -78.847 | 10.486 | 10 | 49.135 | 77.201 |
| 290 | -78.926 | 20.282 | 20 | 66.653 | 68.597 |
| 300 | -78.62 | 30.073 | 30 | 73.08 | 59.205 |
| 310 | -77.798 | 39.846 | 40 | 76.176 | 49.574 |
| 320 | -76.176 | 49.574 | 50 | 77.798 | 39.846 |
| 330 | -73.08 | 59.205 | 60 | 78.62 | 30.073 |
| 340 | -66.653 | 68.597 | 70 | 78.926 | 20.282 |
| 350 | -49.135 | 77.201 | 80 | 78.847 | 10.486 |
| 360 | 0 | 81.893 | 90 | 78.431 | 0.699 |

DATE: 21 MAY 2013

$$
\begin{gathered}
\mathrm{N}=\left(20.16^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -69.874 | 1.2 | 360 | 0 | 73.323 |
| 280 | -70.13 | 10.582 | 10 | 29.524 | 70.683 |
| 290 | -69.562 | 19.963 | 20 | 47.87 | 64.347 |
| 300 | -68.791 | 29.304 | 30 | 57.885 | 56.347 |
| 310 | -66.859 | 38.552 | 40 | 63.541 | 47.623 |
| 320 | -63.541 | 47.623 | 50 | 66.859 | 38.552 |
| 330 | -57.885 | 56.347 | 60 | 68.791 | 29.304 |
| 340 | -47.87 | 64.347 | 70 | 69.562 | 19.963 |
| 350 | -29.524 | 70.683 | 80 | 70.13 | 10.582 |
| 360 | 0 | 73.323 | 90 | 69.874 | 1.2 |

DATE: 21 JUNE 2013

$$
\begin{gathered}
\mathrm{N}=\left(23.45^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.431 | 0.699 | 360 | 0 | 81.893 |
| 280 | -78.847 | 10.486 | 10 | 49.135 | 77.201 |
| 290 | -78.926 | 20.282 | 20 | 66.653 | 68.597 |
| 300 | -78.62 | 30.073 | 30 | 73.08 | 59.205 |
| 310 | -77.798 | 39.846 | 40 | 76.176 | 49.574 |
| 320 | -76.176 | 49.574 | 50 | 77.798 | 39.846 |
| 330 | -73.08 | 59.205 | 60 | 78.62 | 30.073 |
| 340 | -66.653 | 68.597 | 70 | 78.926 | 20.282 |
| 350 | -49.135 | 77.201 | 80 | 78.847 | 10.486 |
| 360 | 0 | 81.893 | 90 | 78.431 | 0.699 |

DATE: 21 JULY 2013

$$
\begin{gathered}
\mathrm{N}=\left(20.46^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -69.575 | 1.217 | 360 | 0 | 73.023 |
| 280 | -69.824 | 10.581 | 10 | 29.055 | 70.427 |
| 290 | -69.485 | 19.943 | 20 | 47.326 | 64.161 |
| 300 | -68.64 | 29.264 | 30 | 57.398 | 56.215 |
| 310 | -66.44 | 38.489 | 40 | 63.117 | 47.53 |
| 320 | -63.117 | 47.53 | 50 | 66.44 | 38.489 |
| 330 | -57.398 | 56.215 | 60 | 68.45 | 29.264 |
| 340 | -47.326 | 64.161 | 70 | 69.485 | 19.943 |
| 350 | -29.055 | 70.427 | 80 | 69.824 | 10.581 |
| 360 | 0 | 73.023 | 90 | 69.575 | 1.217 |

DATE: 21 AUGUST 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.76^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.261 | 0.71 | 360 | 0 | 81.723 |
| 280 | -78.675 | 10.491 | 10 | 49.565 | 77.094 |
| 290 | -78.74 | 20.28 | 20 | 66.222 | 68.537 |
| 300 | -78.436 | 30.065 | 30 | 72.758 | 59.167 |
| 310 | -77.576 | 39.83 | 40 | 75.921 | 49.549 |
| 320 | -75.921 | 49.549 | 50 | 77.576 | 39.83 |
| 330 | -72.758 | 59.167 | 60 | 78.436 | 30.065 |
| 340 | -66.222 | 68.537 | 70 | 78.74 | 20.28 |
| 350 | -49.565 | 77.094 | 80 | 78.675 | 10.491 |
| 360 | 0 | 81.723 | 90 | 0 | 81.723 |

DATE: 21 SEPTEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-0.20^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 89.8 | -0.012 | 180 | 0 | -86.717 |
| 100 | 89.599 | -9.994 | 190 | -72.021 | -79.481 |
| 110 | 88.94 | -19.974 | 200 | -81.087 | -69.745 |
| 120 | 88.226 | -29.953 | 210 | -84.392 | -59.841 |
| 130 | 87.345 | -39.927 | 220 | -86.159 | -49.892 |
| 140 | 86.159 | -49.892 | 230 | -87.345 | -39.927 |
| 150 | 84.392 | -59.841 | 240 | -88.226 | -29.953 |
| 160 | 81.087 | -69.745 | 250 | -88.94 | -19.974 |
| 170 | 72.021 | -79.481 | 260 | -89.599 | -9.994 |
| 180 | 0 | -86.717 | 270 | -89.8 | -0.012 |

DATE: 21 OCTOBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.76^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 78.261 | -0.71 | 180 | 0 | -81.723 |
| 100 | 78.675 | -10.491 | 190 | -49.565 | -77.094 |
| 110 | 78.744 | -20.28 | 200 | -66.222 | -68.537 |
| 120 | 78.422 | -30.065 | 210 | -72.758 | -59.167 |
| 130 | 77.576 | -39.83 | 220 | -75.916 | -49.549 |
| 140 | 75.916 | -49.549 | 230 | -77.576 | -39.83 |
| 150 | 72.758 | -59.167 | 240 | -78.422 | -30.065 |
| 160 | 66.222 | -68.537 | 250 | -78.744 | -20.28 |
| 170 | 49.565 | -77.094 | 260 | -78.675 | -10.491 |
| 180 | 0 | -81.723 | 270 | -78.261 | -0.71 |

DATE: 21 NOVEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-20.46^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 69.575 | -1.217 | 180 | 0 | -73.023 |
| 100 | 69.825 | -10.581 | 190 | -29.555 | -70.427 |
| 110 | 69.485 | -19.943 | 200 | -47.326 | -64.161 |
| 120 | 68.45 | -29.264 | 210 | -57.398 | -56.215 |
| 130 | 66.484 | -38.489 | 220 | -63.117 | -47.53 |
| 140 | 63.117 | -47.53 | 230 | -66.484 | -38.489 |
| 150 | 57.398 | -56.215 | 240 | -68.45 | -29.264 |
| 160 | 47.326 | -64.161 | 250 | -69.485 | -19.943 |
| 170 | 29.055 | -70.427 | 260 | -69.825 | -10.581 |
| 180 | 0 | -73.023 | 270 | -69.575 | -1.217 |

DATE: 21 DECEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-23.45^{\circ}\right) \\
\mathrm{L}=3^{\circ} 29^{\prime}(\text { PEKAN })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 66.569 | -1.387 | 180 | 0 | -70.013 |
| 100 | 66.761 | -10.555 | 190 | -24.932 | -67.799 |
| 110 | 66.294 | -19.715 | 200 | -42.268 | -62.197 |
| 120 | 65.045 | -28.815 | 210 | -52.709 | -54.796 |
| 130 | 62.762 | -37.786 | 220 | -58.959 | -46.516 |
| 140 | 58.959 | -46.516 | 230 | -62.762 | -37.786 |
| 150 | 52.709 | -54.796 | 240 | -65.045 | -28.815 |
| 160 | 42.268 | -62.197 | 250 | -66.294 | -19.715 |
| 170 | 24.932 | -67.799 | 260 | -66.761 | -10.555 |
| 180 | 0 | -70.013 | 270 | -66.569 | -1.387 |

DATE: 21 JANUARY 2013

$$
\begin{gathered}
\mathrm{N}=\left(-20.16^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 69.846 | -0.505 | 180 | 0 | -71.307 |
| 100 | 69.788 | -9.891 | 190 | -26.932 | -68.906 |
| 110 | 69.131 | -19.256 | 200 | -44.92 | -62.955 |
| 120 | 67.755 | -28.557 | 210 | -55.405 | -55.237 |
| 130 | 65.409 | -37.736 | 220 | -61.611 | -46.694 |
| 140 | 61.611 | -46.694 | 230 | -65.409 | -37.736 |
| 150 | 55.405 | -55.237 | 240 | -67.755 | -28.557 |
| 160 | 44.92 | -62.955 | 250 | -69.131 | -19.256 |
| 170 | 26.932 | -68.906 | 260 | -69.788 | -9.891 |
| 180 | 0 | -71.307 | 270 | -69.846 | -0.505 |

DATE: 21 FEBRUARY 2013

$$
\begin{gathered}
\mathrm{N}=\left(-11.24^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\text { JOHOR BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 78.78 | -0.679 | 180 | 0 | -82.243 |
| 100 | 79.202 | -10.477 | 190 | -51.42 | -77.416 |
| 110 | 79.299 | -20.285 | 200 | -67.56 | -68.719 |
| 120 | 79.022 | -30.089 | 210 | -73.751 | -59.282 |
| 130 | 78.254 | -39.877 | 220 | -76.712 | -49.624 |
| 140 | 76.712 | -49.624 | 230 | -78.254 | -39.977 |
| 150 | 73.751 | -59.282 | 240 | -79.022 | -30.089 |
| 160 | 67.56 | -68.719 | 250 | -79.299 | -20.285 |
| 170 | 51.42 | -77.416 | 260 | -79.202 | -10.477 |
| 180 | 0 | -82.243 | 270 | -78.78 | -0.679 |

DATE: 21 MARCH 2013

$$
\begin{gathered}
\mathrm{N}=\left(-0.40^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\text { (JOHOR BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -89.6 | -0.01 | 360 | 0 | 88.128 |
| 280 | -89.335 | 9.986 | 10 | 79.465 | 79.827 |
| 290 | -89.046 | 19.982 | 20 | 84.791 | 69.914 |
| 300 | -88.678 | 29.976 | 30 | 86.645 | 59.944 |
| 310 | -88.256 | 39.97 | 40 | 87.63 | 49.96 |
| 320 | -87.63 | 49.96 | 50 | 88.256 | 39.97 |
| 330 | -86.645 | 59.944 | 60 | 88.678 | 29.976 |
| 340 | -84.791 | 69.914 | 70 | 89.046 | 19.982 |
| 350 | -79.465 | 79.827 | 80 | 89.335 | 9.986 |
| 360 | 0 | 88.128 | 90 | 89.6 | -0.01 |

DATE: 21 APRIL 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.59^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.414 | 0.295 | 360 | 0 | 79.878 |
| 280 | -78.488 | 10.09 | 10 | 44.003 | 75.826 |
| 290 | -78.203 | 19.882 | 20 | 62.117 | 67.725 |
| 300 | -77.486 | 29.656 | 30 | 69.912 | 58.565 |
| 310 | -76.172 | 39.392 | 40 | 73.912 | 49.054 |
| 320 | -73.912 | 49.054 | 50 | 76.172 | 39.392 |
| 330 | -69.912 | 58.565 | 60 | 77.486 | 29.656 |
| 340 | -62.117 | 67.725 | 70 | 78.203 | 19.882 |
| 350 | -44.003 | 75.826 | 80 | 78.488 | 10.09 |
| 360 | 0 | 79.878 | 90 | 78.414 | 0.295 |

DATE: 21 MAY 2013

$$
\begin{gathered}
\mathrm{N}=\left(20.16^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\text { JOHOR BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -69.846 | 0.506 | 360 | 0 | 71.307 |
| 280 | -69.788 | 9.891 | 10 | 26.932 | 68.906 |
| 290 | -69.131 | 19.256 | 20 | 44.922 | 62.956 |
| 300 | -67.755 | 28.557 | 30 | 55.407 | 55.238 |
| 310 | -65.411 | 37.737 | 40 | 61.611 | 46.694 |
| 320 | -61.611 | 46.694 | 50 | 65.411 | 37.737 |
| 330 | -55.407 | 55.238 | 60 | 67.755 | 28.557 |
| 340 | -44.922 | 62.956 | 70 | 69.131 | 19.256 |
| 350 | -26.932 | 68.906 | 80 | 69.788 | 9.891 |
| 360 | 0 | 71.307 | 90 | 69.846 | 0.506 |

DATE: 21 JUNE 2013

$$
\begin{gathered}
\mathrm{N}=\left(23.45^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -66.537 | 0.584 | 360 | 0 | 67.997 |
| 280 | -66.432 | 9.754 | 10 | 23.014 | 65.957 |
| 290 | -65.649 | 18.894 | 20 | 39.835 | 60.676 |
| 300 | -64.06 | 27.948 | 30 | 50.52 | 53.544 |
| 310 | -61.404 | 36.842 | 40 | 57.187 | 45.449 |
| 320 | -57.187 | 45.449 | 50 | 61.404 | 36.842 |
| 330 | -50.52 | 53.544 | 60 | 64.06 | 27.948 |
| 340 | -39.835 | 60.676 | 70 | 65.649 | 18.894 |
| 350 | -23.014 | 65.957 | 80 | 66.432 | 9.754 |
| 360 | 0 | 67.997 | 90 | 66.537 | 0.584 |

DATE: 21 JULY 2013

$$
\begin{gathered}
\mathrm{N}=\left(20.46^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -69.546 | 0.513 | 360 | 0 | 71.007 |
| 280 | -69.484 | 9.88 | 10 | 26.535 | 68.643 |
| 290 | -68.814 | 19.225 | 20 | 44.429 | 62.757 |
| 300 | -67.418 | 28.506 | 30 | 54.946 | 55.092 |
| 310 | -65.043 | 37.661 | 40 | 61.201 | 46.588 |
| 320 | -61.201 | 46.588 | 50 | 65.043 | 37.661 |
| 330 | -54.946 | 55.092 | 60 | 67.418 | 28.506 |
| 340 | -44.429 | 62.757 | 70 | 68.814 | 19.225 |
| 350 | -26.535 | 68.643 | 80 | 69.484 | 9.88 |
| 360 | 0 | 71.007 | 90 | 69.546 | 0.513 |

DATE: 21 AUGUST 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.76^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.244 | 0.299 | 360 | 0 | 79.707 |
| 280 | -78.315 | 10.088 | 10 | 43.512 | 75.705 |
| 290 | -78.023 | 19.874 | 20 | 61.713 | 67.651 |
| 300 | -77.291 | 29.641 | 30 | 69.6 | 58.516 |
| 310 | -75.955 | 39.369 | 40 | 73.656 | 49.02 |
| 320 | -73.656 | 49.02 | 50 | 75.955 | 39.369 |
| 330 | -69.6 | 58.516 | 60 | 77.291 | 29.641 |
| 340 | -61.713 | 67.651 | 70 | 78 | 19.874 |
| 350 | -43.512 | 75.705 | 80 | 78.315 | 10.088 |
| 360 | 0 | 79.707 | 90 | 78.244 | 0.299 |

DATE: 21 SEPTEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-0.20^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 89.8 | -0.005 | 180 | 0 | -88.742 |
| 100 | 89.529 | -9.991 | 190 | -82.901 | -79.922 |
| 110 | 89.714 | -19.999 | 200 | -86.584 | -69.963 |
| 120 | 89.391 | -29.995 | 210 | -87.855 | -59.977 |
| 130 | 89.049 | -39.991 | 220 | -88.603 | -49.986 |
| 140 | 88.603 | -49.986 | 230 | -89.049 | -39.991 |
| 150 | 87.855 | -59.977 | 240 | -89.391 | -29.995 |
| 160 | 86.584 | -69.963 | 250 | -89.714 | -19.999 |
| 170 | 82.901 | -79.922 | 260 | -89.529 | -9.991 |
| 180 | 0 | -88.742 | 270 | -89.8 | -0.005 |

DATE: 21 OCTOBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.76^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\text { JOHOR BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 78.244 | -0.299 | 180 | 0 | -79.707 |
| 100 | 78.315 | -10.088 | 190 | -43.512 | -75.705 |
| 110 | 78.023 | -19.874 | 200 | -61.713 | -67.651 |
| 120 | 77.291 | -29.641 | 210 | -69.6 | -58.516 |
| 130 | 75.957 | -39.369 | 220 | -73.656 | -49.02 |
| 140 | 73.656 | -49.02 | 230 | -75.957 | -39.369 |
| 150 | 69.6 | -58.516 | 240 | -77.291 | -29.641 |
| 160 | 61.713 | -67.651 | 250 | -78.023 | -19.874 |
| 170 | 43.512 | -75.705 | 260 | -78.315 | -10.088 |
| 180 | 0 | -79.707 | 270 | -78.244 | -0.299 |

DATE: 21 NOVEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-20.46^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\text { JOHOR BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 69.546 | -0.513 | 180 | 0 | -71.007 |
| 100 | 69.484 | -9.88 | 190 | -26.535 | -68.643 |
| 110 | 68.814 | -19.225 | 200 | -44.429 | -62.757 |
| 120 | 67.418 | -28.506 | 210 | -54.946 | -55.092 |
| 130 | 65.043 | -37.661 | 220 | -61.201 | -46.588 |
| 140 | 61.201 | -46.588 | 230 | -65.043 | -37.661 |
| 150 | 54.946 | -55.092 | 240 | -67.418 | -28.506 |
| 160 | 44.429 | -62.757 | 250 | -68.814 | -19.225 |
| 170 | 26.535 | -68.643 | 260 | -69.484 | -9.88 |
| 180 | 0 | -71.007 | 270 | -69.546 | -0.513 |

DATE: 21 DECEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-23.45^{\circ}\right) \\
\mathrm{L}=1^{\circ} 28^{\prime}(\mathrm{JOHOR} \text { BHARU })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 66.537 | -0.584 | 180 | 0 | -67.997 |
| 100 | 66.432 | -9.754 | 190 | -23.013 | -65.956 |
| 110 | 65.649 | -18.894 | 200 | -39.835 | -60.676 |
| 120 | 64.061 | -27.949 | 210 | -50.52 | -53.544 |
| 130 | 61.404 | -36.842 | 220 | -57.187 | -45.449 |
| 140 | 57.187 | -45.449 | 230 | -61.404 | -36.842 |
| 150 | 50.52 | -53.544 | 240 | -64.061 | -27.949 |
| 160 | 39.835 | -60.676 | 250 | -65.649 | -18.894 |
| 170 | 23.013 | -65.956 | 260 | -66.432 | -9.754 |
| 180 | 0 | -67.997 | 270 | -66.537 | -0.584 |

DATE: 21 JANUARY 2013
$\mathrm{N}=\left(-20.16^{\circ}\right)$
$\mathrm{L}=6^{\circ} 2^{\prime}$ (KUALA PERLIS)

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 69.956 | -2.207 | 180 | 0 | -76.257 |
| 100 | 70.672 | -11.567 | 190 | -34.278 | -73.176 |
| 110 | 70.834 | -20.951 | 200 | -52.779 | -66.222 |
| 120 | 70.367 | -30.328 | 210 | -61.803 | -57.821 |
| 130 | 69.07 | -39.654 | 220 | -66.521 | -48.862 |
| 140 | 66.521 | -48.862 | 230 | -69.07 | -39.654 |
| 150 | 61.803 | -57.821 | 240 | -70.367 | -30.328 |
| 160 | 52.779 | -66.222 | 250 | -70.834 | -20.951 |
| 170 | 34.278 | -73.176 | 260 | -70.672 | -11.567 |
| 180 | 0 | -76.257 | 270 | -69.956 | -2.207 |

DATE: 21 FEBRUARY 2013

$$
\begin{gathered}
\mathrm{N}=\left(-11.24^{\circ}\right) \\
\left.\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS }\right)
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 78.829 | -1.248 | 180 | 0 | -85.177 |
| 100 | 79.75 | -11.013 | 190 | -63.274 | -79.007 |
| 110 | 80.38 | -20.802 | 200 | -74.868 | -69.665 |
| 120 | 80.712 | -30.605 | 210 | -78.613 | -59.983 |
| 130 | 80.685 | -40.413 | 220 | -80.127 | -50.213 |
| 140 | 80.127 | -50.213 | 230 | -80.685 | -40.413 |
| 150 | 78.613 | -59.983 | 240 | -80.712 | -30.605 |
| 160 | 74.868 | -69.665 | 250 | -80.38 | -20.802 |
| 170 | 63.274 | -79.007 | 260 | -79.75 | -11.013 |
| 180 | 0 | -85.177 | 270 | -78.829 | -1.248 |

DATE: 21 MARCH 2013

$$
\begin{gathered}
\mathrm{N}=\left(-0.40^{\circ}\right) \\
\mathrm{L}=6^{\circ} 25^{\prime}(\text { KUALA PERLIS })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -89.603 | -0.046 | 360 | 0 | 83.177 |
| 280 | -88.461 | 9.89 | 10 | 56.002 | 77.91 |
| 290 | -87.246 | 19.821 | 20 | 71.86 | 68.906 |
| 300 | -85.846 | 29.74 | 30 | 78.272 | 59.293 |
| 310 | -84.119 | 39.639 | 40 | 81.794 | 49.502 |
| 320 | -81.794 | 49.502 | 50 | 84.119 | 39.639 |
| 330 | -78.272 | 59.293 | 60 | 85.846 | 29.74 |
| 340 | -71.86 | 68.906 | 70 | 87.246 | 19.821 |
| 350 | -56.002 | 77.91 | 80 | 88.461 | 9.89 |
| 360 | 0 | 83.177 | 90 | 89.603 | -0.046 |

DATE: 21 APRIL 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.59^{\circ}\right) \\
\left.\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS }\right)
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.481 | 1.287 | 360 | 0 | 84.835 |
| 280 | -79.396 | 11.041 | 10 | 61.677 | 78.858 |
| 290 | -80.009 | 20.819 | 20 | 73.912 | 69.592 |
| 300 | -80.311 | 30.611 | 30 | 77.931 | 59.942 |
| 310 | -80.229 | 40.406 | 40 | 79.591 | 50.192 |
| 320 | -79.591 | 50.192 | 50 | 80.229 | 40.406 |
| 330 | -77.931 | 59.942 | 60 | 80.311 | 30.611 |
| 340 | -73.912 | 69.592 | 70 | 80.009 | 20.819 |
| 350 | -61.677 | 78.858 | 80 | 79.396 | 11.041 |
| 360 | 0 | 84.835 | 90 | 78.481 | 1.287 |

DATE: 21 MAY 2013
$\mathrm{N}=\left(20.16^{\circ}\right)$
$\mathrm{L}=6^{\circ} 2^{\prime}$ (KUALA PERLIS)

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -69.956 | 2.208 | 360 | 0 | 76.26 |
| 280 | -70.672 | 11.567 | 10 | 34.282 | 73.178 |
| 290 | -70.835 | 20.952 | 20 | 52.782 | 66.223 |
| 300 | -70.367 | 30.328 | 30 | 61.809 | 57.823 |
| 310 | -69.07 | 39.654 | 40 | 66.524 | 48.863 |
| 320 | -66.524 | 48.863 | 50 | 69.07 | 39.654 |
| 330 | -61.809 | 57.823 | 60 | 70.367 | 30.328 |
| 340 | -52.782 | 66.223 | 70 | 70.835 | 20.952 |
| 350 | -34.282 | 73.178 | 80 | 70.672 | 11.567 |
| 360 | 0 | 76.26 | 90 | 69.956 | 2.208 |

DATE: 21 JUNE 2013

$$
\begin{gathered}
\mathrm{N}=\left(23.45^{\circ}\right) \\
\left.\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS }\right)
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -66.661 | 2.551 | 360 | 0 | 72.947 |
| 280 | -67.294 | 11.7 | 10 | 28.382 | 70.422 |
| 290 | -67.291 | 20.871 | 20 | 46.335 | 64.298 |
| 300 | -66.554 | 30.018 | 30 | 56.204 | 56.503 |
| 310 | -64.852 | 39.082 | 40 | 61.718 | 47.969 |
| 320 | -61.718 | 47.969 | 50 | 64.852 | 39.082 |
| 330 | -56.204 | 56.503 | 60 | 66.554 | 30.018 |
| 340 | -46.335 | 64.298 | 70 | 67.291 | 20.871 |
| 350 | -28.382 | 70.422 | 80 | 67.294 | 11.7 |
| 360 | 0 | 72.947 | 90 | 66.661 | 2.551 |

DATE: 21 JULY 2013

$$
\begin{gathered}
\mathrm{N}=\left(20.46^{\circ}\right) \\
\left.\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS }\right)
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -69.658 | 2.239 | 360 | 0 | 75.957 |
| 280 | -70.365 | 11.58 | 10 | 33.668 | 72.934 |
| 290 | -70.513 | 20.947 | 20 | 52.155 | 66.059 |
| 300 | -70.019 | 30.304 | 30 | 61.28 | 57.712 |
| 310 | -68.684 | 39.608 | 40 | 66.078 | 48.789 |
| 320 | -66.078 | 48.789 | 50 | 68.684 | 39.608 |
| 330 | -61.28 | 57.712 | 60 | 70.019 | 30.304 |
| 340 | -52.155 | 66.059 | 70 | 70.513 | 20.947 |
| 350 | -33.668 | 72.934 | 80 | 70.365 | 11.58 |
| 360 | 0 | 75.957 | 90 | 69.658 | 2.239 |

DATE: 21 AUGUST 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.76^{\circ}\right) \\
\left.\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS }\right)
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 270 | -78.312 | 1.305 | 360 | 0 | 84.657 |
| 280 | -79.222 | 11.053 | 10 | 60.856 | 78.776 |
| 290 | -79.824 | 20.825 | 20 | 73.416 | 69.551 |
| 300 | -80.111 | 30.612 | 30 | 77.586 | 59.919 |
| 310 | -80.003 | 40.401 | 40 | 79.319 | 50.179 |
| 320 | -79.319 | 50.179 | 50 | 80.003 | 40.401 |
| 330 | -77.586 | 59.919 | 60 | 80.111 | 30.612 |
| 340 | -73.416 | 69.551 | 70 | 79.824 | 20.825 |
| 350 | -60.856 | 78.776 | 80 | 79.222 | 11.053 |
| 360 | 0 | 84.657 | 90 | 78.312 | 1.305 |

DATE: 21 SEPTEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-0.20^{\circ}\right) \\
\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS) }
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 89.801 | -0.023 | 180 | 0 | -83.791 |
| 100 | 89.08 | -9.96 | 190 | -58.484 | -78.247 |
| 110 | 87.891 | -19.894 | 200 | -73.483 | -69.1 |
| 120 | 86.541 | -29.819 | 210 | -79.443 | -59.429 |
| 130 | 84.907 | -39.729 | 220 | -82.725 | -49.609 |
| 140 | 82.725 | -49.609 | 230 | -84.907 | -39.729 |
| 150 | 79.443 | -59.429 | 240 | -86.541 | -29.819 |
| 160 | 73.483 | -69.1 | 250 | -87.891 | -19.894 |
| 170 | 58.484 | -78.247 | 260 | -89.08 | -9.96 |
| 180 | 0 | -83.791 | 270 | -89.801 | -0.023 |

DATE: 21 OCTOBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(11.76^{\circ}\right) \\
\left.\mathrm{L}=6^{\circ} 25^{\prime} \text { (KUALA PERLIS }\right)
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\gamma$ | ALTITUDE <br> ANGLE, $\beta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 78.312 | -1.305 | 180 | 0 | -84.657 |
| 100 | 79.222 | -11.053 | 190 | -60.856 | -78.776 |
| 110 | 79.824 | -20.825 | 200 | -73.416 | -69.551 |
| 120 | 80.111 | -30.612 | 210 | -77.586 | -59.919 |
| 130 | 80.003 | -40.401 | 220 | -79.319 | -50.179 |
| 140 | 79.319 | -50.179 | 230 | -80.003 | -40.401 |
| 150 | 77.586 | -59.919 | 240 | -80.111 | -30.612 |
| 160 | 73.416 | -69.551 | 250 | -79.824 | -20.825 |
| 170 | 60.856 | -78.776 | 260 | -79.222 | -11.053 |
| 180 | 0 | -84.657 | 270 | -78.312 | -1.305 |

DATE: 21 NOVEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-20.46^{\circ}\right) \\
\mathrm{L}=6^{\circ} 25^{\prime}(\text { KUALA PERLIS })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 69.658 | -2.239 | 180 | 0 | -75.957 |
| 100 | 70.365 | -11.58 | 190 | -33.668 | -72.934 |
| 110 | 70.513 | -20.947 | 200 | -52.155 | -66.059 |
| 120 | 70.019 | -30.304 | 210 | -61.28 | -57.712 |
| 130 | 68.684 | -39.608 | 220 | -66.078 | -48.789 |
| 140 | 66.078 | -48.789 | 230 | -68.684 | -39.608 |
| 150 | 61.28 | -57.712 | 240 | -70.019 | -30.304 |
| 160 | 52.155 | -66.059 | 250 | -70.513 | -20.947 |
| 170 | 33.668 | -72.934 | 260 | -70.365 | -11.58 |
| 180 | 0 | -75.957 | 270 | -69.658 | -2.239 |

DATE: 21 DECEMBER 2013

$$
\begin{gathered}
\mathrm{N}=\left(-23.45^{\circ}\right) \\
\mathrm{L}=6^{\circ} 25^{\prime}(\text { KUALA PERLIS })
\end{gathered}
$$

| HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ | HOUR <br> ANGLE, $\boldsymbol{h}$ | AZIMUTH <br> ANGLE, $\boldsymbol{\gamma}$ | ALTITUDE <br> ANGLE, $\boldsymbol{\beta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 66.661 | -2.551 | 180 | 0 | -72.947 |
| 100 | 67.294 | -11.7 | 190 | -28.382 | -70.422 |
| 110 | 67.291 | -20.871 | 200 | -46.335 | -64.298 |
| 120 | 66.64 | -30.018 | 210 | -56.204 | -56.503 |
| 130 | 64.852 | -39.082 | 220 | -61.718 | -47.969 |
| 140 | 61.718 | -47.969 | 230 | -64.852 | -39.082 |
| 150 | 56.204 | -56.503 | 240 | -66.64 | -30.018 |
| 160 | 46.335 | -64.298 | 250 | -67.291 | -20.871 |
| 170 | 28.382 | -70.422 | 260 | -67.294 | -11.7 |
| 180 | 0 | -72.947 | 270 | -66.661 | -2.551 |

## APPENDIX C



## GRAPH OF SUNPATH FOR PERLIS ( $6^{\circ} \mathbf{2 5}$ )



