

A Data Driven Approach to Wind Plant Control using Moth-Flame Optimization (MFO) Algorithm

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Abstract— One of the main issues of the wind plant power generation nowadays is that the current stand alone controller of each turbine in the wind plant is not able to cope with chaotic nature of wake aerodynamic effect. Therefore, it is necessary to re-tune the controller of each turbine in the wind plant such that the total power generation is improved. This article presents an investigation of a data driven approach using moth-flame optimization algorithm (MFO) to the problem of improving wind plants power generation. The MFO based technique is applied to search the turbine's optimum controller such that the aggregation power generation of a wind plant is maximized. The MFO is a population based optimization method that mimics the behavior of moths that navigate on specific angle with respect to the moon location. Here, it is expected that the MFO can solve the control accuracy problem in the existing algorithms for maximizing wind plant. A row of wind turbines plant with wake aerodynamic effect among turbines is adopted to demonstrate the effectiveness of the MFO based technique. The model of the wind plant is derived based on the real Horns Rev wind plant in Denmark. The performance of the proposed MFO algorithm is analyzed in terms of the statistical analysis of the total power generation. Numerical results show that the MFO based approach generates better total wind power generation than spiral dynamic algorithm (SDA) based approach and safe experimentation dynamics (SED) based approach.

Keywords— Moth-flame Optimization (MFO); data driven; wind plant optimization; power generation; alternative energy.

I. INTRODUCTION

These days, wind energy has known to be one of the most economical sources of renewable energy. In recent years, there is a considerable development of wind energy around the world. The main point is to maximize the energy generation of the existing wind plant and minimize the cost-of-energy produced by the wind plants. There are some of the control variables that need to be tuned to achieve the maximization of power generation of the wind plants, such as angle of blade and yaw, and torque generator. Moreover, this tuning variable also plays a significant part in the energy generation of the rear wind turbines because of turbulence or wake interactions between wind turbines. Optimal wind plant operation requires a full understanding of wake interactions as well as the turbine's behavior.

Recently, the optimization of power generation of existing wind plant exhibits a challenging issue which is the complexity of the wake interaction between wind turbines that is difficult to model. This has led to a data-driven approach that is proven as a promising solution to produce the maximum power generation of the wind plant. The data-driven approach will produce desired convergence without requiring characterization of the aerodynamic interaction

among turbines [1]. There are many studies that focus on optimizing the aggregation power generation of wind plant, such as safe experimentation dynamics (SED) method [1]-[3], maximum power point tracking (MPPT) [4]-[5], spiral dynamic algorithm (SDA) [6], simultaneous perturbation stochastic approximation (SPSA) [7], particle swarm optimization (PSO) [8] and random search (RS) [9] algorithms. Note that most of the data-driven methods mostly tackle the problem of improving the power generation of existing installed wind plant, where no modification on the wind turbine position can be done. In particular, we only can improve its control algorithm, such as fine-tune its blade angle or wind turbine yaw angle.

On the other hand, Moth-Flame Optimization (MFO) [10] method, which is introduced by Seyedali Mirjalili in 2015, is also a useful tool for improving the power generation of the wind plant. This is because this technique has been successfully solving various of real-world problems, such as find optimal power flow [11], harmonic elimination of multilevel inverters [12], feature selection problem [13], and multi-objective problem [14], optimal machining parameters in manufacturing processes [15], medical diagnoses [16], tomato disease detection [17], handwritten recognition [18], optical network unit placement [19] and many more. Hence, it is worth to investigate the potential of the MFO based

method in improving the total power generation of the existing wind plant.

This article investigates the effectiveness of moth-flame optimization (MFO) as a data-driven approach for improving the power generation of a row of wind turbines plant. Next, the assessment in terms of mean, best, worst and standard deviation of wind plant power generation is presented. Moreover, the results are also compared with SDA and SED [1] based approaches. The combination of the number of agents or populations and iterations is also investigated since this combination may influence the performance of the algorithm in producing the optimum results.

The structure of this article is organized as follows. Section II explains material and method, which consists of the formulation of the wind plant optimization problem, the MFO algorithm and the procedure to adopt it in a data-driven approach. In Section III, the data-driven based MFO is verified to a row of wind turbines plant. Then, a performance comparison between the MFO, Spiral Dynamic Algorithm, and the Safe Experimentation Dynamics based approaches are also elaborated in Section III. In the final section, we conclude our findings.

II. MATERIAL AND METHOD

A. Problem Formulation

For this study, consider a wind plant with a N number of wind turbines with either random or deterministic formation of wind turbine position. The controller of the turbine k is denoted as s_k ($k = 1, 2, \dots, N$), which is a generic symbol of the turbine regulators, like pitch the angle of the blade and speed of turbine the e motor [20]. The power generation of turbine k is expressed by $J_k(s_1, s_2, \dots, s_N)$ ($k = 1, 2, \dots, N$). The time-varying magnitude of wind speed with different direction is considered in this investigation. Hence, the controller $s_1, s_2, \dots, s_{k-1}, s_{k+1}, \dots, s_N$, which are not included turbine k , might also affect the power generation of turbine k , i.e., J_k . This is due to the aerodynamic interaction among turbines. In the same way, any changes of the controller s_k not only change the power generation J_k but also the power generation of other turbines, i.e., $J_1, J_2, \dots, J_{k-1}, J_{k+1}, \dots, J_N$. Therefore, we can state that the power generation of turbine k is highly affected by the controller s_k and is weakly affected by other controllers, i.e., $s_1, s_2, \dots, s_{k-1}, s_{k+1}, \dots, s_N$. The relation between power generation J_k and controllers s_1, s_2, \dots, s_N is assumed to be unknown since the turbulence behavior between turbines are very complex in reality and it is hard to get a precise wind plant's dynamic model.

Nevertheless, it is assumed that the aggregate power generation of the wind plant is observable where it is expressed by:

$$\bar{J}(s_1, s_2, \dots, s_N) = \sum_{k=1}^N J_k(s_1, s_2, \dots, s_N) \quad (1)$$

Finally, the wind plant control problem is stated by:

Problem 1. Consider the wind plant aggregate power generation $\bar{J}(s_1, s_2, \dots, s_N)$ is given in (1) and let functions

J_k ($k = 1, 2, \dots, N$) are unknown with respect to its controller s_k ($k = 1, 2, \dots, N$). Next, find controller s_k ($k = 1, 2, \dots, N$) such that $\bar{J}(s_1, s_2, \dots, s_N)$ is maximized.

B. Moth-Flame Optimization Algorithm

Firstly, define $f: R^m \rightarrow R$ as a loss function and $P_i \in R^m$ ($i = 1, 2, \dots, n$) is the tuning parameter for n size of populations. Next, for $i = 1, 2, \dots, n$, a maximization problem is given by

$$\max_{P_1, P_2, \dots, P_n} f(P_i). \quad (2)$$

The Moth-Flame Optimization algorithm updates P_i ($i = 1, 2, \dots, n$) using

$$P_i(t+1) = \begin{cases} G_i e^{bo} \cos(2\pi t) + C_j(t), & \text{if } i \leq \text{flame no}, \\ G_i e^{bo} \cos(2\pi t) + C_{\text{flame no}}(t), & \text{if } i > \text{flame no}, \end{cases} \quad (3)$$

where $i = 1, 2, \dots, n$ for $t = 0, 1, \dots$. This equation is referred as the logarithmic spiral equation that used to update the next position for each moth. Here, P_i indicates the moth while

$C_j \in R^m$ ($j = 1, 2, \dots, \text{flame no}$) represents the flame. In particular, if $i \leq \text{flame no}$, then $P_i(t+1)$ is updated according to C_j , where $C_j = C_i \in R^m$, $i = 1, 2, \dots, n$. Meanwhile, for $i > \text{flame no}$, $P_i(t+1)$ is updated according to $C_{\text{flame no}}$. The symbol G_i represents the displacement between the i^{th} moth and the j^{th} flame, which is calculated as follows:

$$G_i = |C_j(t) - P_i(t)|. \quad (4)$$

In equation (3), b is a constant for describing the shape of the logarithmic spiral, while o is a generated random number between y to 1, where y is linearly decreasing gain from -1 to -2 iteratively, as shown in (5)

$$y = -1 + t \times \left(\frac{-1}{t_{\max}} \right). \quad (5)$$

Here, t is the current number of iteration and t_{\max} is the maximum number of iterations. In order to get high exploitation of the promising solutions, the number of flames with respect to the iteration number is proposed as below:

$$\text{flame no} = \text{round} \left(C_{\max} - t \times \frac{C_{\max} - 1}{t_{\max}} \right) \quad (6)$$

where C_{\max} is maximum number of flames, t is the current number of iteration and t_{\max} is the maximum number of iteration. Then, the procedure of the MFO algorithm is given by:

Step 1: Determine the size of populations n , maximum number of iterations t_{\max} and the constant b . Let algorithm start with $t = 0$.

III. RESULTS AND DISCUSSION

Step 2: Determine the first tuning parameter $P_i(0) \in R^m$, $i = 1, 2, \dots, n$ arbitrarily in a searching space. Compute the flame number equation in (6). Then, sort $P_i(0)$ in descending order where from higher value of objective function to lower value of objective function and find the best solution P^* . Here, $P^* = P_{i_c}(0)$ for $i_c = \arg \max_i f(P_i(0))$, $i = 1, 2, \dots, n$. Next, store the result at $C_i(0) \in R^m$, $i = 1, 2, \dots, n$. Proceed with step 4.

Step 3: Compute the *flame no* at (4). Next, merge $P_i(t-1)$ and followed by $C_i(t-1)$ as follows

$$\text{merged population} = \begin{bmatrix} P_1 \\ P_2 \\ \vdots \\ P_n \\ C_1 \\ C_2 \\ \vdots \\ C_n \end{bmatrix} \quad (7)$$

then sort *merged population* in descending order where from higher value of objective function to lower value of objective function. Select the best n positions from *merged population* as the flame and store the result at $C_i(t) \in R^m$, $i = 1, 2, \dots, n$. Find the best solution, P^* in $P^* = P_{i_c}(t)$, where $i_c = \arg \max_i f(P_i(t))$, $i = 1, 2, \dots, n$.

Step 4: Execute the MFO algorithm in (3).

Step 5: Update $t = t + 1$. Proceed Step 3 if a termination criterion t_{max} is not achieved. In another way, the procedure terminates with the optimal tuning parameter P^* .

In Step 5, the termination of the procedure is selected from the maximal iterations, where the procedure terminates once a pre-specified t_{max} is achieved. In this case, a preliminary trials is performed to observe its convergence curve in order to decide the maximum iteration.

C. Data Driven Design

Note that the presented MFO algorithm in Section II-B is generic algorithm that can be applied for many engineering optimization problems. Therefore, another procedure is required to apply the MFO algorithm for wind plant optimization problem. By applying the MFO technique in the previous section, the data driven MFO based technique for finding the optimal controller of wind plant power generation is given by:

Procedure I: Determine the number of iterations t_{max} .

Procedure II: Apply the MFO procedure in Section II-B by denoting $\bar{J} = f$ and $s = P_i$.

Procedure III: This data-driven procedure terminates after t_{max} . The optimal controller $s^* = P^*$ and the corresponding aggregate power generation \bar{J} is observed.

Now, we validate the data-driven based MFO algorithm in improving wind plant power generation. Initially, a wind plant model that represents an actual wind plant is adopted to assess the data-driven method. Here, the model of the wind plant, which is take from [20] is explained. Next, the MFO algorithm technique is used to a row wind plant model.

A. Dynamic Model of Wind Plant

Let $x = 1, 2, \dots, n$, be the set of n turbines in the wind plant, the approaching wind speed is defined by V_ω , the diameter of turbine motor is denoted by D_k , the region of motor swept of turbine l is defined by A_l . The roughness coefficient that depicts the gradient of wake propagation is denoted by the symbol \emptyset , the overlay area between the turbine k wake and turbine l motor swing area is defined by $A_{k \rightarrow l}^{ov}$. The notation (z, r_ω) is represented as a center point in the wake of the turbine with z is the length to the turbine motor circle plane and r_ω is the length to the center of the turbine motor axis. Next, the resultant wind speed is given by:

$$\bar{V}_l = V_\omega \left[1 - 2 \sqrt{\sum_{k \in X: Z_k < Z_l} \left(q_k \left(\frac{D_k}{D_k + 2\emptyset(z_l - z_k)} \right)^2 \frac{A_{k \rightarrow l}^{ov}}{A_l} \right)^2} \right] \quad (8)$$

where z_k is the length to the turbine k motor circle plane, while z_l is the length to the turbine l motor circle plane. Figure 1 depicts the demonstration of wake interaction between the two turbines. For $l \in x$, the wind speed \bar{V}_l is computed based on the wind speed resultant deficit generated by each front turbine. We assume that the wake grows proportionally to the length z and its diameter has a round cross-section. Note that, in reality, we may not expect an ideal proportionality of wake with round cross-section. Furthermore, the individual turbine power is expressed by:

$$J_l = 2\rho A_l s_l (1 - s_l)^2 \bar{V}_l^3 \quad (9)$$

where ρ is the air density.

Remark 1. Note that, in this study, our proposed data-driven MFO only use the measurable total power generation without even know the detailed model of wind plant in (8) and (9). In order to represent this dynamic model of the wind plant, the algorithm will capture the data of total power aggregation after the incoming wind has pass through all the turbines from the first row until the final row. In that case, our proposed method has a good potential to be applied in actual wind plant system since the data-driven MFO only capture the total power data without even know the complex aerodynamic interactions amongst turbines.

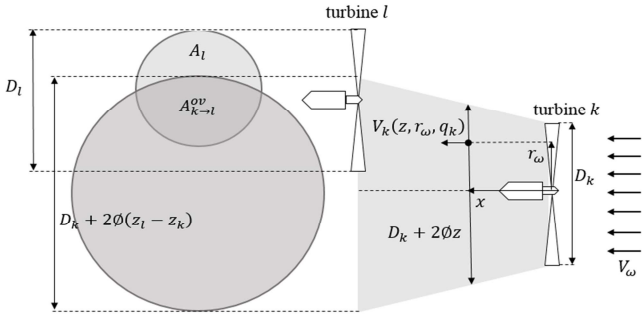


Fig.1 The diagram of wake interaction

B. Numerical Evaluation

The performance of the MFO based algorithm is demonstrated using a ten turbines row of wind plant, which is illustrated in Figure 2. The diameter of each wind turbine is 80 m. The length between each turbine is equivalent to the total diameter of seven turbines, which is 560 m. Other coefficients of wind plant, such as air density ρ , roughness coefficient ϕ is taken from [7]. In this study, the

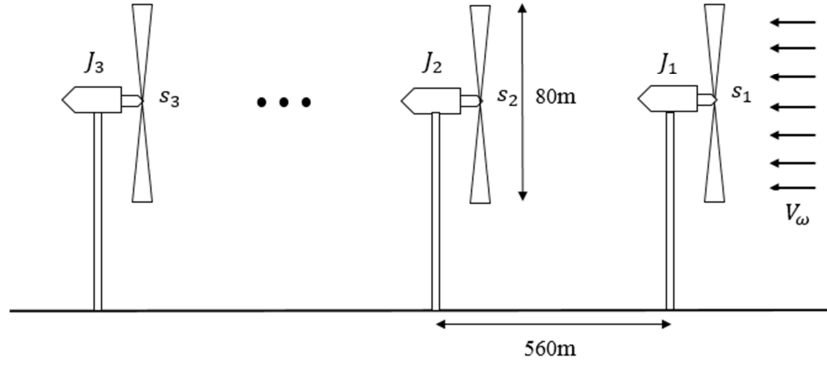


Fig.2A row of wind turbines

Here, 10000 number of evaluations is allocated for MFO, SDA and SED based approaches such that a fair comparative assessment is obtained. For SED based approach, we set $t_{max} = 10000$ because it only needs single evaluation or one experiment per iteration while for the SDA based approach and the MFO based approach, $t_{max} = 200$ and $n = 50$ are chosen. Note that the combination of maximum number of iteration and size of population is selected such that a better total power generation is obtained.

Figures 3 and 4 show the result of the simulation by using MATLAB, for the wind plant total power generation responses of MFO and SDA based approaches after 500 iterations by using 20 number of agents. From the graph pattern, it is observed that the loss function response of the MFO based approach is as good as SDA based approach. Meanwhile, Figure 5 demonstrates the simulation result of total power generation by using SED based approach. Since SED based approach is a single search agent, we set $t_{max} = 10000$. The simulation starts at $t = 0$ and stop after t reaches 10000, where the optimal design parameter is obtained.

performance of the MFO, is benchmarked with the SDA based method and SED based method.

Firstly, the wind speed is assumed to be constant at $V_m = 8$ m/s. Then, MFO coefficients are set after run for several preliminary experiments, where b is set between 0.75 to 1.0 with 0.05 increment. The coefficients of SDA based approach is denoted by $r = 0.97$ and $\alpha = \pi/4$. Meanwhile, the coefficients of SED based approach with updated step size $K_G = 0.03$ and the probability to update the tuning parameter $E = 0.3$ are used. Note that the MFO based method only requires one pre-defined parameter b ; while the SDA and SED based methods require two pre-defined parameters. Hence, the MFO based method requires less effort to fine tune the pre-defined parameter. The initial controller value of each turbine is set between 0 and 0.3333. In order to observe the stochastic behavior in the proposed approaches, 100 trials are performed to MFO, SED and SDA based approaches.

Table 1 tabulates the statistical evaluation of the aggregate power generation for MFO based approach after 10000 evaluations. The optimal value of b is selected based on the maximum value for the best, mean and worst of total power generation and minimum value of standard deviation. Notice that there are four data that reach higher best total power generation (4.7648415724 MW) which are $b = 0.95, 0.80, 0.75$, and 0.70 . Moreover, $b = 0.95$ produces slightly lower standard deviation value than other b values. This shows that the best value of b for defining the shape of logarithmic spiral is $b = 0.95$. Table 2 tabulates the total power generation analysis of MFO based approach compared to SDA and SED based approaches. It is clearly shown that the MFO based method yields higher best total power generation (4.7648415724MW) than the SDA (4.7648415723MW) and SED (4.7644075485MW) based approaches. The average and lowest values of the total power generation also shows the same pattern. MFO algorithm also reaches lowest standard deviation than the SDA and SED based approaches. This result verifies that MFO algorithm can achieve maximum total power generation consistently.

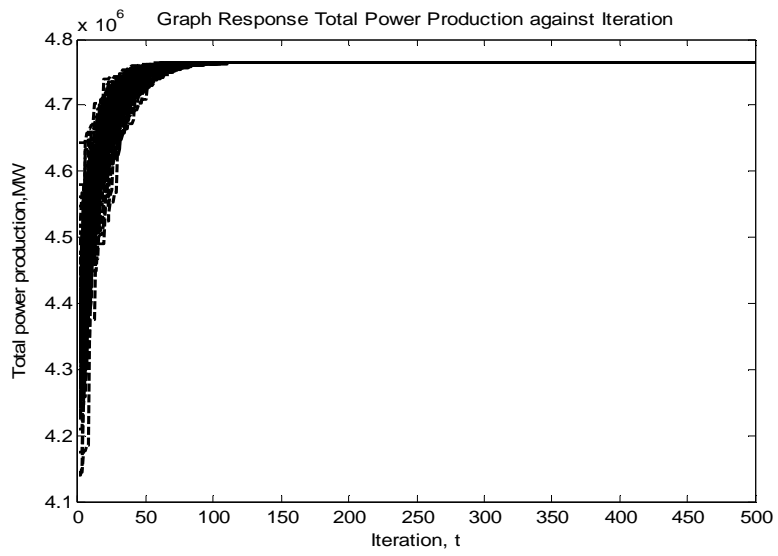


Fig.3 Graph Response Total Power Generation of MFO algorithm

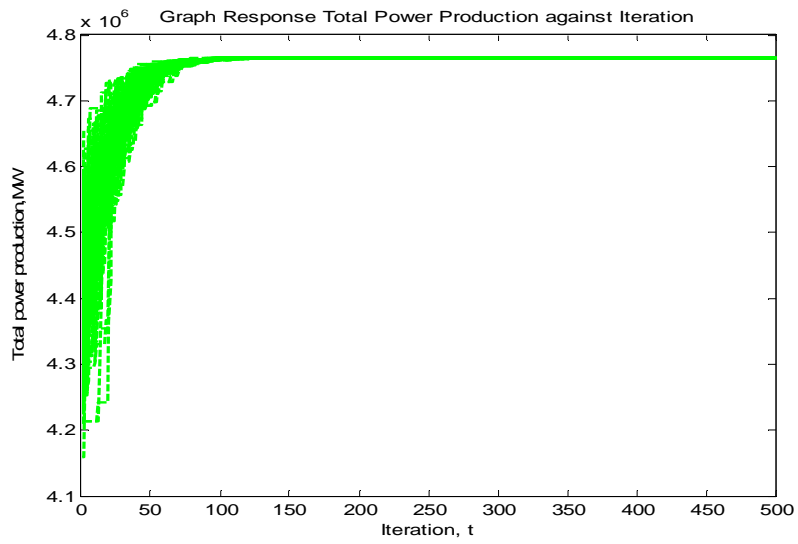


Fig.4 Graph Response Total Power Generation of SDA algorithm

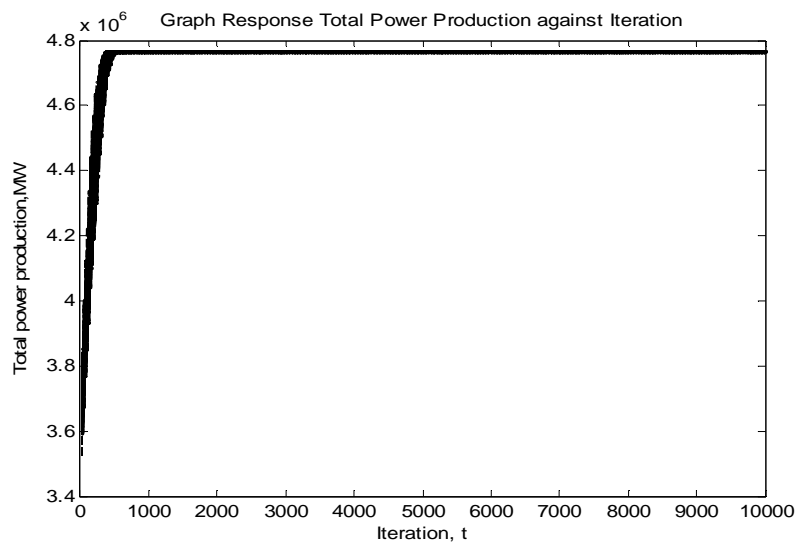


Fig.5 Graph Response Total Power Generation of SED algorithm

TABLE I
PERFORMANCE COMPARISON OF TOTAL POWER GENERATION FOR
DIFFERENT VALUE OF b

b	Mean (MW)	Best (MW)	Worst (MW)	Standard Deviation
1.00	4.7641691656	4.7648415724	4.6976008998	6.7241e+03
0.95	4.7648415724	4.7648415724	4.7648415724	5.6161e-10
0.90	4.7630743588	4.7648415724	4.6764808948	1.2433e+04
0.85	4.7641691656	4.7648415724	4.6976008999	6.7241e+03
0.80	4.7648415724	4.7648415724	4.7648415724	4.3903e-10
0.75	4.7648415724	4.7648415724	4.7648415724	3.7441e-10
0.70	4.7648415724	4.7648415724	4.7648415724	3.7441e-10

TABLE II
THE COMPARISON PERFORMANCE OF TOTAL POWER GENERATION (MW)
BETWEEN MFO, SDA AND SED BASED APPROACH

Statistical Evaluation	MFO	SDA	SED
Average	4.7648415724	4.7648415723	4.7644075485
Highest	4.7648415724	4.7648415723	4.7648415242
Lowest	4.7648415724	4.7648415723	4.7627457259
Standard Deviation	5.6161×10^{-10}	1.1039824×10^{-7}	4.513106×10^2

IV. CONCLUSION

This paper presents a data-driven method based on moth-flame optimization (MFO) algorithm has been investigated. This study aims to propose a MFO for a power generation of wind plant and compare the findings with SDA and SED based approaches. In this simulation results, the MFO based method exhibits a slightly higher total power generation than the SDA and SED based approaches. This proves the potential of MFO based approach for data driven method of wind plant control. In the future, it is necessary to improve the convergence speed of MFO since it will take longer time if the size of wind plant is large. In this case, one might consider a multi-resolution version of MFO to increase the convergence speed.

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