



# Optimal placement and sizing of FACTS devices for optimal power flow using metaheuristic optimizers



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## ARTICLE INFO

### Keywords:

Cost minimization  
Loss minimization  
Metaheuristic algorithms  
Optimal power flow  
FACTS devices

## ABSTRACT

This paper proposes the implementation of various metaheuristic algorithms in solving the optimal power flow (OPF) with the presence of Flexible AC Transmission System (FACTS) devices in the power system. OPF is one of the well-known problems in power system operations and with the inclusion of the FACTS devices allocation problems into OPF will make the solution more complex. Thus, seven metaheuristic algorithms: Barnacles Mating Optimizer (BMO), Marine Predators Algorithm (MPA), Moth-Flame Optimization (MFO), Particle Swarm Optimization (PSO), Gravitational Search Algorithm (GSA), Teaching-Learning-Based Optimization (TLBO) and Heap-Based Optimizer (HBO) are used to solve two objective functions: power loss and cost minimizations. These algorithms are selected from the different metaheuristics classification groups, where the implementation of these algorithms into the said problems will be tested on the modified IEEE 14-bus system. From the simulation results, it is suggested that TLBO and HBO perform better compared to the rest of algorithms.

## 1. Introduction

In modern power system planning and operations, the Optimal Power Flow (OPF) emerged as one of the complex problems to be solved. It is expected that the power system needs to be operated at optimal condition so that the maximum security and reliability can be achieved. OPF problem solution involving the non-convex, large scale and non-linear constrained optimization problems. It is aimed to find the optimal control variables of power systems' components such as real power generations, generator's voltages, transformers setting, reactive compensation elements etc. so that the minimization of objective functions can be obtained. In addition, electronically controlled Flexible AC Transmission System (FACTS) devices can mitigate most of the problems associated with power quality and overload in the power network. Proper allocation of these devices may increase the efficient utilization of the existing facilities [1]. Thus, the optimal solution that integrating the FACTS devices' allocation into OPF problems becoming one of interesting research topics to be addressed since the implementation of FACTS devices has been proved to improve the power quality of the power system network [2,3].

To date, there are various approached to solve OPF with the presence of FACTS devices that have been proposed in literature mainly using metaheuristic such as Particle Swarm Optimization (PSO) [4], Opposition Krill Herd Algorithm (OKHA) [5], Symbiotic Organisms Search (SOS) [6], Efficient Parallel Genetic Algorithm (EPGA) [7], Success History-based Adaptive Differential Evolution (SHADE) [1], Integrated Ant Lion Optimizer (IALO) and Grasshopper Optimization Algorithm (GOA) called as IALGOA [8] and many more apart from using the conventional techniques such as sequential quadratic programming that has been proposed in [9] and Newton method which has been proposed in [10].

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In related works for metaheuristic algorithms' performance in solving engineering problems, several comparative studies have been discussed and performed such as in [11–18]. From the literature reviews, it can be noticed that the application of metaheuristic algorithms into engineering problems is ever-increasing interest, year by year especially in OPF solution. Thus, this paper proposes an application of seven recent metaheuristic algorithms namely Barnacles Mating Optimizer (BMO), Marine Predator Algorithm (MPA), Moth–Flame Optimization (MFO), Particle Swarm Optimization (PSO), Gravitational Search Algorithm (GSA), Teaching–Learning-Based Optimization (TLBO) and Heap Based Optimizer (HBO) to solve OPF problem which considering the presence of FACTS devices in the power system network. The contributions of this paper can be listed as follow:

- The implementation of seven selected metaheuristic algorithms into OPF solution on the well-known IEEE 14-bus system with considering the integration of FACTS devices allocation problem.
- Conducting comparative studies among seven recent metaheuristic algorithms in the OPF solution field.
- Four cases of single objective of OPF solution by metaheuristic algorithms: loss and cost minimizations problems.

The rest of the paper is organized as follows: Section 2 discusses the OPF formulation followed by the brief description of seven metaheuristic algorithms in Section 3. The implementation of selected metaheuristic algorithms in solving OPF is presented in Section 4 and followed by the simulation studies in Section 5. Finally, Section 6 states the conclusion of this paper.

## 2. Optimal power flow problem formulation

The main purpose of OPF is to find the optimal setting of control variables in power system components to minimize the selected objective functions while satisfying all the equality and inequality constraints. In this paper, two objectives are identified to solve OPF for the system that considering the allocation problem of FACTS devices: (1) loss minimization and (2) cost of generation minimization.

### 2.1. Minimization of power loss

The first objective function is the total power loss minimization,  $F_{Loss}$ , as follows:

$$F_{Loss} = \sum_{i=j}^{nl} \sum_{j \neq i}^{nl} G_{ij} \left[ V_i^2 + V_j^2 - 2V_i V_j \cos(\delta_i - \delta_j) \right] \quad (1)$$

where  $nl$  is the number of transmission line of the power system,  $G_{ij}$  is the conductance at the transmission line  $i$ - $j$ ,  $V_i$ ,  $\delta_i$ ,  $V_j$  and  $\delta_j$  are the sending end voltage, phase angle of sending end, receiving end voltage, and phase angle of receiving ends respectively.

### 2.2. Minimization of generation cost

Second objective function that consider in this paper is the total cost that include the valve loading effects,  $F_{Cost}(P_{Gi})$ , which is expressed as follows:

$$F_{Cost}(PT_G) = \sum_{i=1}^{N_G} a_i + b_i P_{Gi} + c_i P_{Gi}^2 + \left| d_i \cdot \sin \left[ e_i \cdot (P_{Gi}^{min} - P_{Gi}) \right] \right| \quad (2)$$

where  $PT_G$  is the total power output of generators,  $a_i$ ,  $b_i$ ,  $c_i$ ,  $d_i$  and  $e_i$  denote the cost coefficients of respected generator  $P_{Gi}$  with valve loading effect consideration and  $P_{Gi}^{min}$  is the minimum setting of power of  $i$ -th generator.

### 2.3. Model of FACTS devices

In this paper, three FACTS devices will be considered which are Static VAR compensator (SVC), Thyristor-Controlled Series Compensation (TCSC) and Thyristor Controlled Phase Shifter (TCPS). Shunt compensation device SVC supplements the reactive power of the system while TCSC and TCPS are the series compensation devices which are used to enhance the loading capability and power flow of the line. Basically, the modeling of these devices are based on [1].

For SVC, it consists of a fixed capacitor with a thyristor-controlled reactor. The reactance is varied by controlling the thyristor firing angle. SVC can be utilized for both inductive and capacitive compensation. In power flow study, reactive power provided by SVC,  $Q_{SVC}$  can be expressed as follows:

$$Q_{SVC} = -V_i^2 \cdot B_{SVC} \quad (3)$$

where  $B_{SVC}$  is the equivalent susceptance.

For TCSC on the other hand, it consists of a fixed series capacitor ( $X_C$ ) in parallel with a thyristor-controlled reactor ( $X_L$ ). Similar with [1], the reactance is considered as  $X_C < X_L$  so that the TCSC acts as a variable capacitive reactance. The inductive reactance is varied by controlling the firing angle of the thyristors ( $\gamma$ ). The effective reactance of TCSC can be expressed as follows:

$$X_{TCSC}(\gamma) = \frac{X_C X_L(\gamma)}{X_L(\gamma) - X_C} \quad (4)$$

The modified equivalent reactance ( $X_{eq}$ ) of the transmission line after incorporating TCSC can be expressed as follows:

$$X_{eq} = (1 - \tau)X_{ij} \quad (5)$$

where  $\tau = \frac{X_{TCSC}}{X_{ij}}$ , which is termed as the degree of series compensation with  $X_{ij}$  being the line inductive reactance. The power flow equations of the line incorporating

TCSC as well as the model of TCPS integration into the existing system can be obtained in details in [1].

## 2.4. Constraints

In solving the OPF problem, all the feasible solutions need to fulfill all the equality and inequality constraints. For equality constraint, the power balance equation for real and reactive power must be satisfied and expressed as follow:

$$P_{Gi} - P_{Di} - V_i \sum_{j=1}^{nB} V_j Y_{ij} \cos(\theta_{ij} + \delta_i - \delta_j) = 0 \quad \forall i \in nB \quad (6)$$

$$Q_{Gi} - Q_{Di} - V_i \sum_{j=1}^{nB} V_j Y_{ij} \sin(\theta_{ij} + \delta_i - \delta_j) = 0 \quad \forall i \in nB \quad (7)$$

where  $P_{Gi}$  and  $Q_{Gi}$  are the real and reactive power generation at bus  $i$ ,  $P_{Di}$  and  $Q_{Di}$  are the real and reactive load at bus  $i$  and  $nB$  is the total number of buses in the system.

When the FACTS devices are considered, the following equality constraints are used:

$$P_{Gi} + P_{is} - P_{Di} - V_i \sum_{j=1}^{nB} V_j Y_{ij} \cos(\theta_{ij} + \delta_i - \delta_j) = 0 \quad \forall i \in nB \quad (8)$$

$$Q_{Gi} + Q_{is} + Q_{SVCi} - Q_{Di} - V_i \sum_{j=1}^{nB} V_j Y_{ij} \sin(\theta_{ij} + \delta_i - \delta_j) = 0 \quad \forall i \in nB \quad (9)$$

where  $P_{is}$  and  $Q_{is}$  are the active and reactive power respectively, injected by the TCPS at bus  $i$  [1] and  $Q_{SVCi}$  is the injected reactive power at bus  $i$  by the SVC.

The inequality constraint on the other hand, are the operating limits of the power system components which can represented as follow:

$$P_{Gi}^{min} \leq P_{Gi} \leq P_{Gi}^{max} \quad i = 1, \dots, N_G \quad (10)$$

$$Q_{Gi}^{min} \leq Q_{Gi} \leq Q_{Gi}^{max} \quad i = 1, \dots, N_G \quad (11)$$

$$V_{Gi}^{min} \leq V_{Gi} \leq V_{Gi}^{max} \quad i = 1, \dots, N_G \quad (12)$$

$$V_{Li}^{min} \leq V_{Li} \leq V_{Li}^{max} \quad i = 1, \dots, N_{Load} \quad (13)$$

$$Q_{Ck}^{min} \leq Q_{Ck} \leq Q_{Ck}^{max} \quad k = 1, \dots, N_{QC} \quad (14)$$

$$T_l^{min} \leq T_l \leq T_l^{max} \quad l = 1, \dots, N_T \quad (15)$$

$$\text{SVC: } Q_{SVC}^{min} \leq Q_{SVC} \leq Q_{SVC}^{max} \quad (16)$$

$$\text{TCSC: } \Phi_{TCSC}^{min} \leq \Phi_{TCSC} \leq \Phi_{TCSC}^{max} \quad (17)$$

$$\text{TCPS: } \tau_{TCPS}^{min} \leq \tau_{TCPS} \leq \tau_{TCPS}^{max} \quad (18)$$

where (10) and (11) represent the real and reactive power generations limits for thermal generation, respectively. Constraints on voltage of generator buses is expressed in (12), while (13) defined as the voltage limits at load buses with  $N_G$  is the number of generator and  $N_{Load}$  is the number of load buses. The limitation of injected MVAR and transformer tap setting are shown in (14) and (15), respectively while  $N_{QC}$  is the total number of injected MVAR and  $N_T$  is the number of transformers in the system network.

It is worth to mention that all these constraints are satisfied by using the power flow program (MATPOWER) [19] to ensure the accurate results can be obtained.

## 3. Metaheuristic algorithms

### 3.1. Barnacles mating optimizer

Barnacles Mating Optimizer (BMO) has been proposed by [20–22] where it mimics the mating concept of barnacles. Barnacles are hermaphroditic organisms where they have both male and female reproduction organs. They are mating in two ways which are by copulate with the near neighbors by knocking their penis to allow the mating process and there is rare probability of sperm cast mating, where this is happened for isolate barnacles. These behaviors are inspired for exploitation and exploration process to be included in the BMO for solving optimization problems. In BMO, the exploitation process is adopted the concept of Punnet square

by Hardy–Weinberg principle and the exploration process is adopted from sperm-cast mating. Only one parameter needs to be tuned namely  $pl$ , apart of number of population and maximum iteration in BMO. The concept of exploitation and exploration proposed in BMO can be obtained in details in [20].

### 3.2. Marine Predators Algorithm (MPA)

Next bio-inspired algorithm that will be used for solving OPF problem with FACTS devices is called Marine Predators Algorithm (MPA) that has been proposed in [23]. This algorithm is based on the marine behavioral of ocean predators by imposing the Brownian and Levy motions concepts in the algorithm. It follows the rules that naturally govern in optimal foraging strategy and encounters rate policy between predator and prey in marine ecosystem. The three phases of optimization are schematically proposed which are (1) prey movement using Brownian motion for exploration phase followed by (2) predator starts searching for its prey in Brownian motion while prey switches to Levy to efficiently search its close neighborhood and (3) finally the predator starts switching its behavior from Brownian to Levy strategy to more efficiently search a certain neighborhood. Another point which causes a behavioral change in marine predators is environmental issues such as the eddy formation or Fish Aggregating Devices (FADs) effects. The FADs are considered as local optima and their effect as trapping in these points in search space. Consideration of these longer jumps during simulation avoids stagnation in local optima.

### 3.3. Moth–Flame optimization (MFO)

Moth–Flame Optimization (MFO) algorithm is inspired from the moths' navigation method at night by maintaining a fixed angle with respect to the moon called transverse orientation proposed by Mirjalili [24]. However, they are trapped in a useless or deadly spiral path around artificial lights. In MFO, a logarithmic spiral equation is used for evaluating the moths' movement because it dictates how the moths update their positions around flames. The spiral equation allows a moth to fly "around" a flame and not necessarily in the space between them, where from this condition the exploration and exploitation of the search space can be guaranteed. It is assumed that the candidate solutions are moths and the problem's variables are the position of moths in the space. Therefore, the moths can fly in 1-D, 2-D, 3-D, or hyper dimensional space with changing their position vectors due to the MFO algorithm is also known as one of the population-based algorithms.

### 3.4. Particle Swarm Optimization (PSO)

The comparison performance of the OPF analysis is not complete if not comparing the performance using the Particle Swarm Optimization (PSO) algorithm. PSO is the most well-known algorithm that forming the Swarm Intelligence (SI) group of metaheuristic algorithms in solving optimization problems. It has been invented by Eberhart and Kennedy in 1995 where the algorithm is based on the social behavior of animals like a flock of birds or school of fishes [25]. PSO introduces the position and velocity of particles swarm in finding the optimal solution where it become the major influence in enhancing the exploitation and exploration abilities in searching for the optimality. All these particles will move within the searching space towards the location of food (optimal location) in a specific speed and continuously change their respective positions to arrive at the destination. Their movement is guided by their own experience namely  $P_{best}$ , and the experience of the other particles in a group known as  $G_{best}$ . Each particle will update its velocity as well as its position in order to obtain the next best search solution. In PSO, there are five parameters need to set viz. inertia weight,  $w$ , acceleration coefficients for cognitive and social components,  $c_1$  and  $c_2$ , and independently random vectors,  $r_1$  and  $r_2$  which are uniform distributed random numbers between [0, 1].

### 3.5. Gravitational Search Algorithm (GSA)

Gravitational Search Algorithm (GSA) is inspired by the law of Newtonian gravity and mass interaction. It can be categorized as physics-based metaheuristic algorithm and the algorithm is proposed in 2009 by [26] where can be recognized as the first algorithm to solve optimization problem that fall under this category. In GSA, each mass (agent or candidate of solution) has four specifications: position, inertial mass, active gravitational and passive gravitational masses. The position of the mass corresponds to a solution of the problem and its gravitational and inertia masses are determined using a fitness or objective functions. Each mass is treated as a solution and the optimal solution is navigated by properly adjusting the gravitational and inertia masses. By lapse of time, it is expected that masses be attracted by the heavier mass and this mass can be considered as an optimum solution in the search space. The GSA could be considered as an isolated system of masses, which is like a small artificial world of masses obeying the Newtonian laws of gravitation and motion.

### 3.6. Teaching-Learning Based Optimization (TLBO)

A TLBO is inspired by the teaching and learning process in the classroom invented by [27,28] where later had numerous debate regarding the discrepancies arose such as the terms, flowchart, pseudo code and the program code as mentioned in [29,30]. Nevertheless, as far as NFL theorem is concerned, the different types of setting and problems also can give different results and interpretations. Thus, this work is using the program that has been developed by [31] which has catered all the issues raised by [29].

Similar with other metaheuristic algorithms, TLBO uses population-based solution where the population is treated as a group or a class of learners, the design variables are analogues to subjects offered to learners and the learners' result is analogues to the

'fitness'. The process of acquiring knowledge is divided into teacher and learner phases and the teacher is considered as the best solution so far [32]. This algorithm can be said classified as a non-parameter algorithm since apart of number of population and maximum iteration, there is no parameter need to be adjusted or tuned to obtain the optimal results. This algorithm is fall under human-based metaheuristic algorithm group.

### 3.7. Heap-Based Optimizer (HBO)

Heap-Based Optimizer (HBO) utilizes the heap data structure to map the concept of Corporate Rank Hierarchy (CRH) [33]. HBO can be classified as human-based metaheuristic algorithm group. The development of HBO is based on three pillars, which are the interaction between the subordinates and their immediate boss, the interaction between the colleagues, and self-contribution of the employees in the corporate company. The primary objective of this CRH is giving the formal activities an organized shape and achieving the end goals optimally. CRH manifests the population while the search agent represents a heap node. The search agent's fitness is the master of the heap node, and the population index of the search agent is the value of the heap node. In HBO, to obtain an appropriate balance between exploration and exploitation, the mathematical equations are carefully derived from three major CRH activities. In addition, a self-adaptive parameter called Gamma is designed to escape local optima and avoid premature convergence without compromising the exploitation capability of the HBO.

## 4. Metaheuristic optimizers for OPF solution with FACTS devices allocation problem

In general, OPF solution can be defined as follows:

$$\begin{aligned} & \text{Minimize } F(x, u) \\ & s.t \quad g(x, u) = 0 \\ & \quad \quad h(x, u) \leq 0 \end{aligned} \quad (19)$$

where  $F(x, u)$  is the objective function,  $g(x, u)$  is the equality constraints and  $h(x, u)$  is the inequality constraints.  $x$  and  $u$  are the control and state variables respectively since in power system, to obtain the optimality, not only the control variable; the state variables also play a vital role for the security of the power system operation. In this paper, four case studies will be implemented on IEEE 14-bus system where the OPF with FACTS devices will be solved by all six selected metaheuristic algorithms, as follows:

Case 1: OPF problems with SVC and TCSC for loss minimization

Case 2: OPF problems with SVC and TCPS for loss minimization

Case 3: OPF problems with SVC and TCSC for cost minimization

Case 4: OPF problems with SVC and TCPS for cost minimization

So, the set of control and state variables in OPF solution can be expressed as follow:

$$x^T = \left[ P_{G_2} \cdots P_{G_{NG}}, V_{G_1} \cdots V_{G_{NG}}, T_1 \cdots T_{NT}, Bus_{SVC}, Q_{SVC}, Branch_{TCSC/TCPS}, \Phi_{TCSC}/\tau_{TCPS} \right] \quad (20)$$

$$u^T = \left[ P_{G_1}, Q_{G_1} \cdots Q_{G_{NG}}, V_{L_1} \cdots V_{L_{NL}} \right] \quad (21)$$

where  $P_{G_1}$  is the slack bus generation,  $P_{G_i}$  = the real power generation at voltage controlled buses at the slack bus,  $V_{G_i}$  = the voltage magnitude at voltage controlled buses,  $T_i$  = the tap settings of transformer,  $Bus_{SVC}$  is the location of the SCV to be installed,  $Q_{SVC}$  = the shunt injected VAR,  $Branch_{TCSC/TCPS}$  is the location of TCSC or TCPS at which branch to be installed,  $V_{L_i}$  = the voltage magnitude at load buses and  $Q_{G_i}$  is the reactive power generation for all generator units.

The application of the selected metaheuristic optimizers in solving OPF problem is to find the optimal values of control variables to minimize all the objective functions that have been discussed in previous section while fulfilling all the constraints. Initially, number of search agents or population and the maximum iteration are set. Then, all the function details such as boundary of searching areas and the function evaluation (minimization of objective functions) are determined. Each set of solution are mapped into the load flow data and load flow MATPOWER program is executed to obtain the selected objective (Cases 1 and 2). It is worth to highlight that the penalty function is enforced for the violation of inequality constraints of real power at slack bus, voltage magnitude at load buses and reactive power generations, which can be expressed as follows:

$$penalty = \lambda_P (P_{G_1} - P_{G_1}^{lim})^2 + \lambda_V \sum_{i=1}^{NL} (V_{L_i} - V_{L_i}^{lim})^2 + \lambda_Q \sum_{i=1}^{NG} (Q_{G_i} - Q_{G_i}^{lim})^2 \quad (22)$$

where  $\lambda_P$ ,  $\lambda_V$ , and  $\lambda_Q$  are the penalty factors. General flow of metaheuristic optimizers' application into OPF problem is depicted in Fig. 1.

## 5. Results and discussion

*Case 1: OPF problems with SVC and TCSC for loss minimization*

Simulations for solving OPF are executed using MATLAB and the modified IEEE 14-bus system is used for all cases. IEEE 14-bus system can be considered as small-scale problem that consists of 14 buses, 5 generators, 3 transformers and 11 loads. The modification is to change the synchronous compensator at buses 3, 6 and 8 to a thermal generator as shown in Fig. 2. As both the location and rating of FACTS devices are yet to be optimized, those are indicated with dotted lines in the diagram.

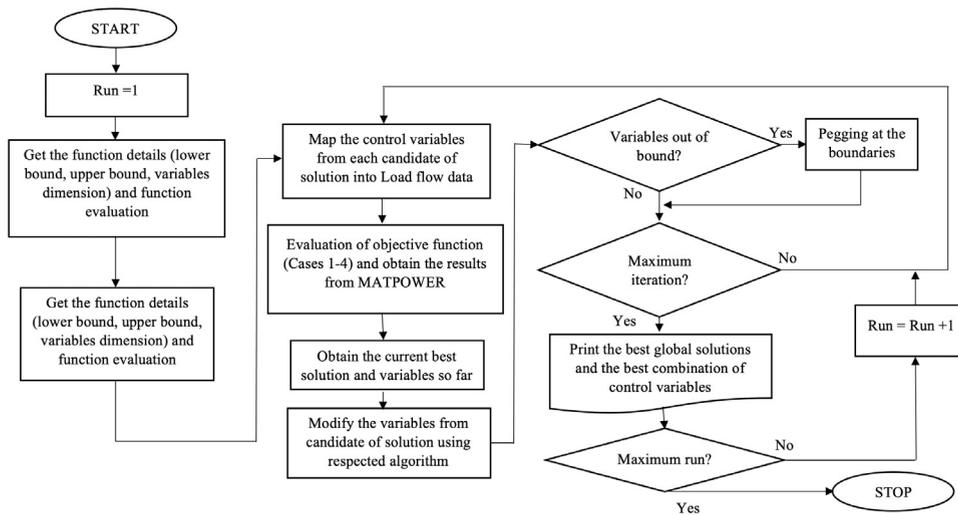


Fig. 1. Flow of metaheuristic algorithms for solving OPF problem with FACTS devices' allocation.

Table 1  
Coefficients for thermal generators for modified IEEE 14-bus system.

Generator	Bus	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>
$T_{G1}$	1	0	20	0.0430292599	18	0.037
$T_{G2}$	2	0	20	0.25	16	0.038
$T_{G3}$	3	0	40	0.01	12	0.045
$T_{G4}$	6	0	40	0.01	13.5	0.041
$T_{G5}$	8	0	40	0.01	13.5	0.041

All simulations for solving OPF problem with FACTS devices using all metaheuristic optimizers are implemented using MATLAB on a MacBook Pro Processor 2.40 GHz Quad-Core Intel Core i5, 8 GB RAM. For all four cases, the control variables to be optimized is 16 variables that consist of the components that have been discussed previously. Table 1 shows the coefficients of thermal generators with valve-loading effects. The population of all algorithms is set to 30 and the maximum iteration is set to 100. For all simulations, 16 control variables need to be optimized that consist of real power generation, voltage at generator buses, transformers tap setting and FACTS devices' allocation while the number of state variables are 15 viz. real power generation at slack bus, reactive power generation and voltage at load buses. All these setting have been used for all cases to obtain fair results for all simulations. It is worth to mention that the following assumptions have been made while adding the FACT devices [1]:

- SVC is not installed on generator buses as the generator itself can exchange reactive power.
- TCSC/ TCPS are not installed on branches having tap changing transformers.

Table 2 shows the detail results of the control variables with slack generator at bus 1 as well as reactive power generations obtained by all algorithms viz. BMO, MPA, MFO, PSO, GSA, TLNO and HBO. These results are the best result obtained from 30 free running of simulations. From this table, it can be seen that TLBO outperformed other compared algorithms which is highlighted in boldface. TLBO achieved the minimum total power loss, 0.918 MW and the second-best result is obtained by MFO which produced 0.949 MW. The difference results obtained between TLBO with the MFO is 0.031 MW. The worst result is obtained by GSA where the significant loss minimization from TLBO compared to GSA is about 49% reduction of power loss. This shows the effectiveness of TLBO compared to other algorithms. It is worth to mention that the total power loss for original condition without optimization of OPF and FACTS devices' allocation is 10.218 MW. Thus, from the simulations that have been conducted, it can be concluded that this is tremendous improvement of power loss reduction.

It also can be noted from the table that all algorithms gave the optimal results within the specified limits that have been set for the simulation. Most algorithms determined the SVC are located at bus 14 which are resulted from BMO, PSO, TLBO and HBO while MPA and MFO suggested the SVC should located at bus 13. Only GSA proposed to install the SVC at bus 7. These locations are not installed at generator buses. For TCSC, the location for install it varies for all algorithms which contributed significantly different for minimizing the power loss for this system. The convergence curve for all algorithms in solving this case is depicted in Fig. 3. It can be concluded that all algorithms are converged within 100 iterations.

Case 2: OPF problems with SVC and TCPS for loss minimization

In this case, the TCPS is considered that replacing the TCSC as in Case 1, where the optimal location and angle of TCPS be optimized by all algorithms. Table 3 shows the best of detail results obtained for all algorithms in 30 runs of simulation. Again, it can be noted that TLBO outperformed other compared algorithms in terms of obtaining the minimum loss production, which is highlighted in boldface. For this case, it can be noted that all algorithms able to obtain the optimal results within the boundaries,

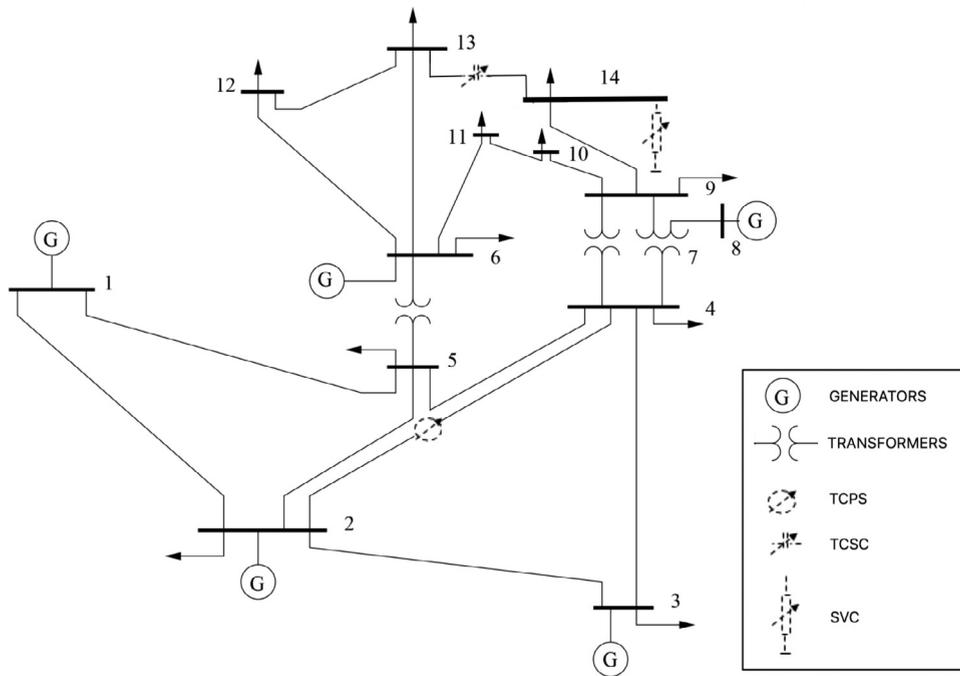


Fig. 2. Modified IEEE 14-bus system.

Table 2  
Detail results for different algorithms on Case 1.

Control variables	Min	Max	BMO	MPA	MFO	PSO	GSA	TLBO	HBO
$P_{G2}$	10	140	10.0000	12.9168	10.0000	11.6665	32.3766	10.0000	10.0000
$P_{G3}$	10	100	88.7592	92.3804	100.0000	78.8669	59.3109	82.4516	82.1314
$P_{G6}$	10	100	32.5512	35.4701	28.4597	39.7532	46.8738	34.1794	38.4139
$P_{G8}$	10	100	78.4944	69.1903	71.4546	79.1750	61.3109	83.2532	79.1186
$V_1$	0.95	1.1	1.0613	1.0624	1.0516	1.0709	1.0445	1.0649	1.0293
$V_2$	0.95	1.1	1.0521	1.0545	1.0430	1.0630	1.0338	1.0561	1.0234
$V_3$	0.95	1.1	1.0433	1.0522	1.0449	1.0550	1.0224	1.0503	1.0146
$V_6$	0.95	1.1	0.9824	1.0260	1.0486	1.0351	1.0304	1.0371	1.0262
$V_8$	0.95	1.1	0.9583	1.0392	1.0579	1.0297	1.0245	1.0590	1.0174
$T_{4-7}$	0.9	1.1	1.1	1.06	1.04	1.1	1.04	1	1
$T_{4-9}$	0.9	1.1	0.9	0.96	0.9	0.9	1	1	0.98
$T_{5-6}$	0.9	1.1	1.1	1	0.98	1	0.98	1	0.98
SVC bus no.			14	13	13	14	7	14	14
$Q_{SVC}$ (MVAR)	-10	10	10.0000	9.9587	7.6357	4.0764	-0.9047	2.0756	10.0000
TCSC branch			13 (6-13)	20 (13-14)	2 (1-5)	3 (2-3)	12 (6-12)	11 (6-11)	20 (13-14)
$\tau_{TCSC_1}$ (%)	0	50%	0.12	0.19	0.17	0.02	0.23	0.50	0.10
Loss (MW)			1.013	0.958	0.949	0.95	1.784	<b>0.918</b>	0.969
State variables									
$P_{G1}$	50	332.4	50.21	50	50.03	50.49	60.91	50.03	50.31
$Q_{G1}$	-40	50	2.08	0.10	0.98	0.28	2.72	1.41	-4.85
$Q_{G2}$	-40	40	5.05	0.51	-3.81	6.19	-3.84	1.32	10.23
$Q_{G3}$	-6	40	13.59	16.10	17.80	15.44	16.65	15.53	13.46
$Q_{G6}$	-6	24	23.47	0.14	5.70	8.14	15.37	11.27	11.47
$Q_{G8}$	-6	24	1.14	16.90	16.22	16.72	15.02	14.39	7.47

whether for control variables as well as for state variables. The convergence curve for all algorithms in solving this case is depicted in Fig. 4. It can be seen that GSA converged too soon which is less than 10 iterations which resulted the worst results compared to others.

Case 3: OPF problems with SVC and TCSC for cost minimization

For this case, the minimization of generator cost is considered as stated in Eq. (2) which including the valve-loading effects of the power generation. The control variables to be optimized is similar with Case 1, only the objective now is to find minimum cost generation. Detail optimal results obtained by all algorithms are tabulated in Table 4, where the best cost minimization is achieved by TLBO which is 5943.47 \$/hour and the worst result is obtained by GSA, 5978.56 \$/hour. The difference results obtained between

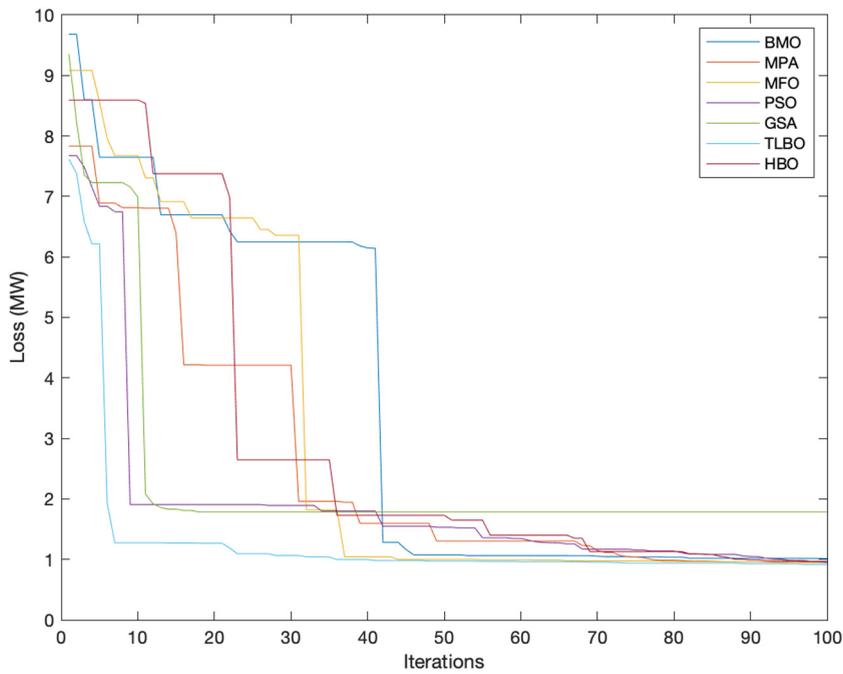


Fig. 3. Convergence curve for all algorithms of Case 1.

Table 3  
Detail results for different algorithms on Case 2.

Control variables	Min	Max	BMO	MPA	MFO	PSO	GSA	TLBO	HBO
$P_{G2}$	10	140	10.0000	14.8119	10.0000	10.0000	38.4064	10.2753	10.0000
$P_{G3}$	10	100	84.2983	96.6241	80.3790	85.0134	59.2636	87.6470	91.0320
$P_{G6}$	10	100	35.2974	23.2973	19.5523	47.4428	42.3520	33.3663	34.1893
$P_{G8}$	10	100	80.0688	75.2264	99.7471	67.4491	62.1601	78.6063	74.6654
$V_1$	0.95	1.1	0.9819	1.0484	1.0380	1.0506	1.0299	1.0575	1.0462
$V_2$	0.95	1.1	0.9734	1.0406	1.0277	1.0414	1.0204	1.0489	1.0380
$V_3$	0.95	1.1	0.9620	1.0396	1.0192	1.0448	1.0113	1.0437	1.0340
$V_6$	0.95	1.1	1.0447	1.0593	1.0342	1.0107	1.0275	1.0462	0.9794
$V_8$	0.95	1.1	1.0547	1.0685	1.0408	1.0239	1.0252	1.0617	1.0093
$T_{4-7}$	0.9	1.1	0.9	1	0.94	1	0.98	0.98	1.02
$T_{4-9}$	0.9	1.1	0.9	0.94	1.02	1.1	1	0.98	1.04
$T_{5-6}$	0.9	1.1	0.92	0.96	1	1.02	0.96	1	1.06
SVC bus no.			4	14	7	10	9	7	13
$Q_{SVC}$ (MVAR)			5.4418	5.9269	10.0000	6.1182	1.3519	-8.0615	7.7771
TCPS branch			20 (13-14)	15 (7-9)	15 (7-9)	15 (7-9)	11 (6-11)	15 (7-9)	4 (2-4)
$\Phi$ TCSPS(deg.)	-5	5	1.1121	1.0517	4.4096	-2.3108	0.3972	0.4510	0.3412
Loss (MW)			1.0397	0.9605	0.9815	1.0367	1.9184	<b>0.9384</b>	0.9835
State variables									
$P_{G1}$	50	332.4	50.38	50.00	50.30	50.13	58.74	50.04	50.10
$Q_{G1}$	-40	50	0.80	0.01	3.97	0.39	3.67	1.01	-0.44
$Q_{G2}$	-40	40	9.84	-0.66	1.22	-8.76	4.80	2.19	1.08
$Q_{G3}$	-6	40	11.97	16.00	14.35	22.66	24.45	15.81	15.14
$Q_{G6}$	-6	24	14.64	8.61	23.34	15.16	18.29	19.90	11.33
$Q_{G8}$	-6	24	6.38	13.51	3.26	9.29	13.32	14.60	13.12

TLBO with the GSA is 35.09 \$/hour which is significant about  $\$35.09/\text{hour} \times 8760 \text{ h} (24 \text{ hour/day} \times 365 \text{ days}) = \$ 307,388.40$  cost saving per year. From this table also, it can be seen that the results obtained by PSO violating the minimum state variable's limit for reactive power generation at bus 6 viz.  $Q_{G6}$  which is highlighted in red boldface.

The location for SVC installation is varied obtained by all algorithms where TLBO and HBO locate at bus 14, while MFO and PSO decided to install the SVC at bus 4. For TCSC location, MPA, MFO, TLBO and HBO gave the similar results where the TCSC need to be installed at branch 3 (line 2-3), while others gave varies results. The convergence curve for this case is plotted in Fig. 5 where all algorithms converged within less than 70 iterations.

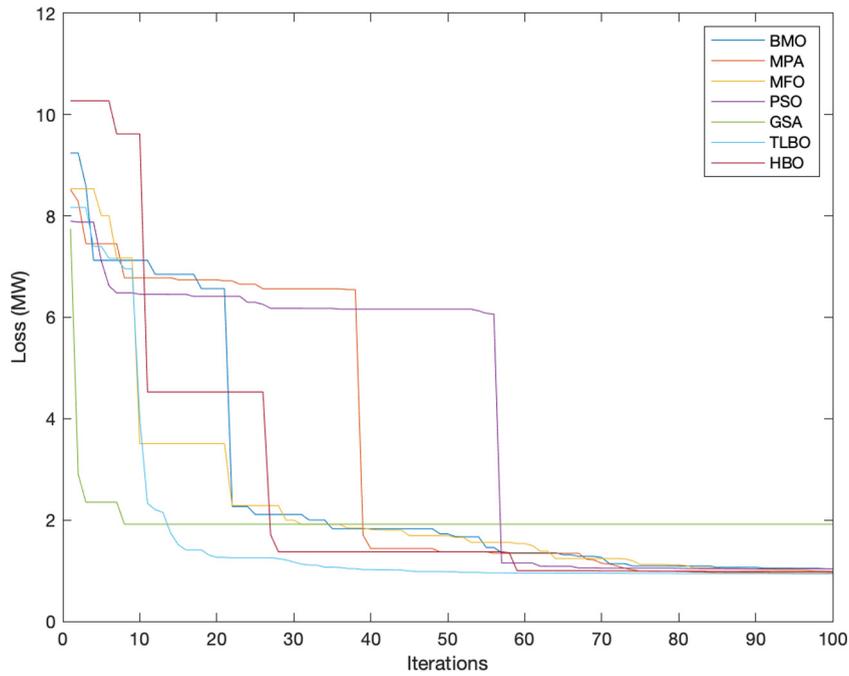


Fig. 4. Convergence curve for all algorithms of Case 2.

Table 4  
Detail results for different algorithms on Case 3.

Control variables	Min	Max	BMO	MPA	MFO	PSO	GSA	TLBO	HBO
$P_{G2}$	10	140	101.5744	101.4882	101.4663	101.5536	81.1452	101.4167	101.3172
$P_{G3}$	10	100	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000
$P_{G6}$	10	100	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000
$P_{G8}$	10	100	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000
$V_1$	0.95	1.1	1.0903	1.1000	1.1000	1.1000	1.0873	1.0997	1.0953
$V_2$	0.95	1.1	1.0802	1.0855	1.0839	1.0913	1.0712	1.0868	1.0838
$V_3$	0.95	1.1	1.0459	1.0520	1.0486	1.0613	1.0335	1.0554	1.0512
$V_6$	0.95	1.1	1.0399	1.0182	1.0611	1.1000	1.0027	1.0605	1.0643
$V_8$	0.95	1.1	1.0668	1.0012	1.0622	1.1000	1.0225	1.0635	1.0681
$T_{4-7}$	0.9	1.1	0.98	1.1	1.1	1.04	1.04	1	1.06
$T_{4-9}$	0.9	1.1	1.04	0.92	0.9	0.9	0.96	1.02	0.94
$T_{5-6}$	0.9	1.1	1.02	1.02	0.98	0.9	1.02	0.96	0.96
SVC bus no.			7	10	4	4	9	14	14
$Q_{SVC}$ (MVAR)	-10	10	-10.0000	4.4615	-10.0000	10.0000	-1.3232	10.0000	7.1425
TCSC branch			1 (1-2)	3 (2-3)	3 (2-3)	20 (13-14)	7 (4-5)	3 (2-3)	3 (2-3)
$\tau$ TCSC <sub>1</sub> (%)	0	50%	0.00	0.28	0.27	0.00	0.23	0.29	0.25
Cost (\$/hr)			5947.30	5944.87	5944.33	5946.23	5978.56	<b>5943.47</b>	5943.61
State variables									
$P_{G1}$	50	332.4	134.94	134.91	134.90	134.91	156.22	134.91	135.02
$Q_{G1}$	-40	50	-6.90	4.68	7.79	-5.58	4.70	1.89	-2.73
$Q_{G2}$	-40	40	23.22	18.70	14.48	28.47	29.57	18.80	19.26
$Q_{G3}$	-6	40	21.63	21.70	18.16	25.11	22.56	22.88	19.69
$Q_{G6}$	-6	24	20.35	8.81	12.66	<b>-13.69</b>	14.99	-3.20	-0.11
$Q_{G8}$	-6	24	11.94	2.36	19.20	15.02	13.68	3.80	13.73

Case 4: OPF problems with SVC and TCPS for cost minimization

In this case, the setting for control and state variables are similar with the Case 2 and the objective function is similar with Case 3. The detail results of simulation for this case are depicted in Table 5. From this table, it can be noted that HBO outperformed others by obtaining the minimum cost of generation which is 5944.09 \$/hour. The next best result is obtained by MFO followed by TLBO, MPA, PSO and finally GSA. From this table also can be noted that the state variable for  $Q_{G6}$  by PSO and GSA is violated the minimum boundary setting. The convergence curve for this case is shown in Fig. 6 where all algorithms converged within less than 90 iterations.

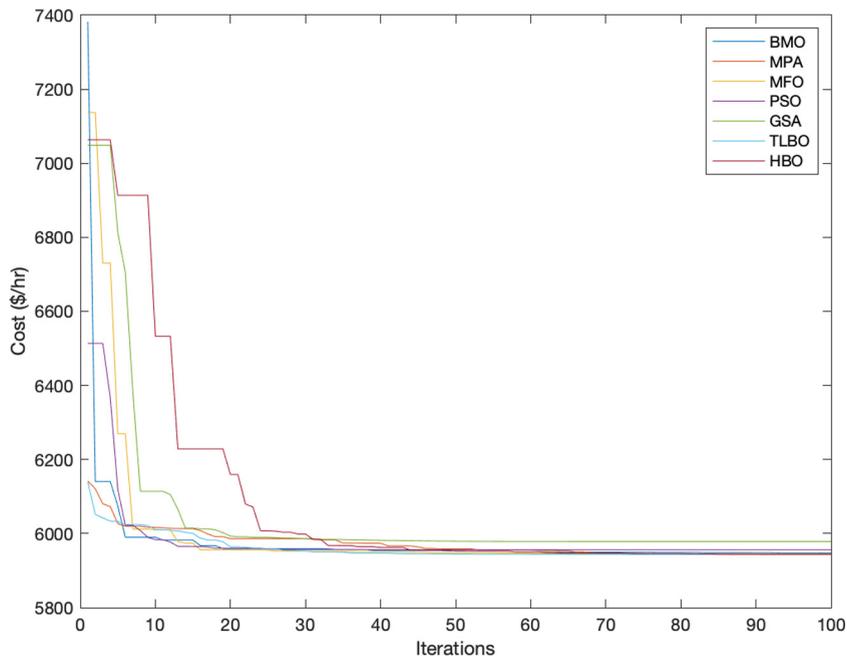


Fig. 5. Convergence curve for all algorithms of Case 3.

Table 5

Detail results for different algorithms on Case 4.

Control variables	Min	Max	BMO	MPA	MFO	PSO	GSA	TLBO	HBO
$P_{G2}$	10	140	101.4401	101.5148	101.4998	101.9774	85.8511	101.4947	101.4576
$P_{G3}$	10	100	10.0060	10.0000	10.0000	10.0000	10.0000	10.0000	10.0000
$P_{G6}$	10	100	10.0000	10.0000	10.0000	10.0000	10.0000	10.0002	10.0000
$P_{G8}$	10	100	10.0000	10.0000	10.0000	10.0000	10.0000	10.0003	10.0003
$V_1$	0.95	1.1	1.1000	1.0983	1.1000	1.1000	1.0636	1.0967	1.0934
$V_2$	0.95	1.1	1.0838	1.0846	1.0838	1.0894	1.0495	1.0839	1.0797
$V_3$	0.95	1.1	1.0449	1.0487	1.0488	1.0581	1.0193	1.0510	1.0442
$V_6$	0.95	1.1	1.0301	1.0528	1.0244	1.0732	1.0228	1.0548	1.0561
$V_8$	0.95	1.1	1.0376	1.0539	1.0359	1.0739	1.0328	1.0682	1.0478
$T_{4-7}$	0.9	1.1	1.1	1.08	1.08	1.1	1.02	1	1.06
$T_{4-9}$	0.9	1.1	0.94	0.9	0.98	0.9	1	1.02	0.92
$T_{5-6}$	0.9	1.1	1	0.98	1	0.9	1.06	0.98	1
SVC bus no.			14	4	14	4	7	4	13
QSVC (MVAR)			5.5973	2.5071	6.2399	9.9900	-2.4268	0.5953	9.6657
TCPS branch			1 (1-2)	1 (1-2)	3 (2-3)	20 (13-14)	11 (6-11)	1 (1-2)	6 (3-4)
$\Phi$ TCSPS(deg.)	-5	5	0.38	0.75	-2.00	5.00	1.81	1.40	-2.01
Cost (\$/hr)			5945.79	5945.27	5944.34	5954.96	5974.59	5945.05	<b>5944.09</b>
State variables									
$P_{G1}$	50	332.4	134.99	134.9	134.87	134.91	151.57	134.91	134.9
$Q_{G1}$	-40	50	8.50	3.35	8.02	0.51	-8.13	1.38	0.15
$Q_{G2}$	-40	40	14.21	17.92	13.19	29.01	6.26	16.67	14.99
$Q_{G3}$	-6	40	15.35	19.07	18.76	24.88	20.84	22.03	17.78
$Q_{G6}$	-6	24	4.06	6.40	1.83	<b>-18.61</b>	<b>38.70</b>	8.96	9.15
$Q_{G8}$	-6	24	14.54	12.84	12.87	20.77	9.72	8.39	7.89

For further analyzing the performance of all algorithms in solving the OPF with FACTS devices' allocation problems, the statistical results for all cases are recoded and presented in Table 6. From this table, it can be concluded that TLBO performed better in most of the cases especially in cases 1 and 2 while HBO able to perform better in case 4. Even though HBO performed better in case 3 for maximum and mean results, TLBO is the best in finding the minimum cost of generation in case 3. Overall, the TLBO and HBO produce very competitive performance and outperformed most of the algorithms for all cases.

### 6. Conclusion

In this paper, seven metaheuristic algorithms namely BMO, MPA, MFO, PSO, GSA TLBO and HBO have been proposed to solve OPF with the FACTS allocation problems. To analyze and assess the performance of all algorithms in solving the problems, they have

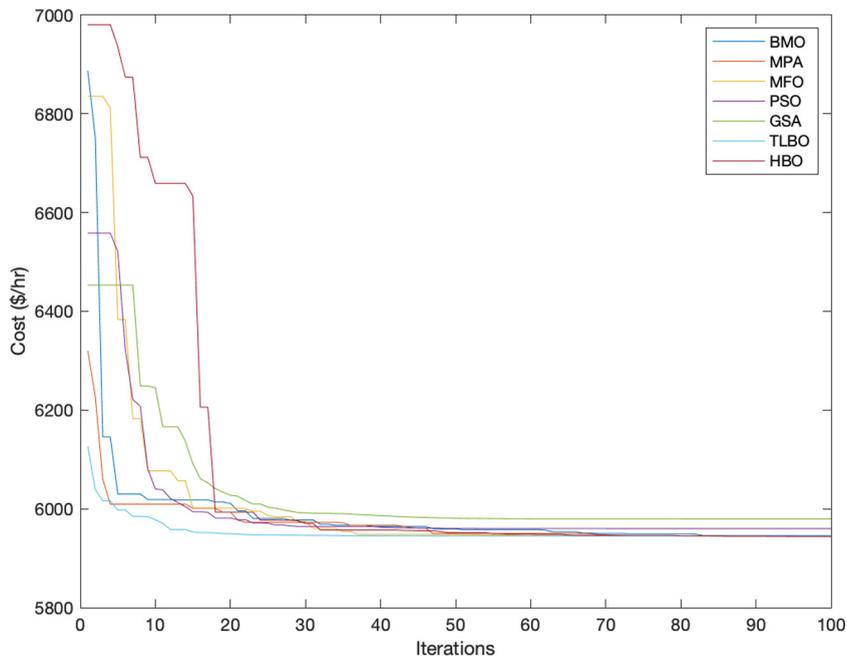


Fig. 6. Convergence curve for all algorithms of Case 4.

**Table 6**  
Statistical results for different algorithms on all cases.

Case	Statistical	BMO	MPA	MFO	PSO	GSA	TLBO	HBO
Case 1	Min	1.0128	0.9580	0.9485	0.9496	1.7843	<b>0.9178</b>	0.9693
	Max	3.1459	1.1476	3.1784	1.8373	4.6530	<b>1.0989</b>	1.5959
	Mean	1.3678	1.0266	1.3529	1.3160	2.6493	<b>0.9954</b>	1.1579
	Std Dev.	0.5094	<b>0.0460</b>	0.4178	0.2424	0.5270	0.0498	0.1405
Case 2	Min	1.0397	0.9605	0.9815	1.0367	1.9184	<b>0.9384</b>	0.9835
	Max	1.9611	1.2155	2.1340	2.1959	2.9145	<b>1.1074</b>	1.4250
	Mean	1.2613	1.0455	1.2469	1.3484	2.2952	<b>1.0010</b>	1.1316
	Std Dev.	0.2025	0.0631	0.2676	0.2375	0.2408	<b>0.0456</b>	0.1118
Case 3	Min	5947.3039	5944.8731	5944.3298	5956.2265	5978.5605	<b>5943.4727</b>	5943.6109
	Max	6005.0696	5950.7428	5958.9405	6396.1937	6845.4320	6025.7163	<b>5949.3704</b>
	Mean	5972.1610	5946.8668	5948.8930	6031.1177	6436.6284	5982.8453	<b>5945.8152</b>
	Std Dev.	17.9978	<b>1.0714</b>	3.8833	92.0980	226.4421	30.9961	1.1595
Case 4	Min	5945.7940	5945.2709	5944.3410	5959.9625	5979.5883	5945.0462	<b>5944.0926</b>
	Max	6015.2284	<b>5954.0831</b>	5959.3588	6056.7575	6976.2456	6029.1131	5955.0994
	Mean	5969.1528	5947.5460	5950.0005	6006.6263	6493.3314	5993.2388	<b>5946.8637</b>
	Std Dev.	17.0312	<b>2.3427</b>	3.7261	32.3930	255.3215	24.1129	2.4264

been applied on two OPF objective functions viz. transmission loss as well as generation cost on modified IEEE 14-bus system through four cases. Statistical and comparative analysis show that TLBO and HBO produce very competitive performance and outperformed the rest of algorithms for most of the cases. Therefore, they can be an effective alternative for solving OPF problem with the presence of FACTS devices.

**Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

**References**

[1] Biswas PP, Arora P, Mallipeddi R, Suganthan PN, Panigrahi BK. Optimal placement and sizing of FACTS devices for optimal power flow in a wind power integrated electrical network. *Neural Comput Appl* 2021;33(12):6753–74. <http://dx.doi.org/10.1007/s00521-020-05453-x>, 06/01 2021.

[2] Ashok Kumar L, Indragandhi V. Power quality improvement of grid-connected wind energy system using facts devices. *Int J Ambient Energy* 2020;41(6):631–40. <http://dx.doi.org/10.1080/01430750.2018.1484801>, 05/11 2020.

- [3] Kullay Reddy DC, Narayana SS, Ganesh V. Towards an enhancement of power quality in the distribution system with the integration of BESS and FACTS device. *Int J Ambient Energy* 2019;1–9. <http://dx.doi.org/10.1080/01430750.2019.1636866>.
- [4] Naderi E, Pourakbari-Kasmaei M, Abdi H. An efficient particle swarm optimization algorithm to solve optimal power flow problem integrated with FACTS devices. *Appl Soft Comput* 2019;80:243–62. <http://dx.doi.org/10.1016/j.asoc.2019.04.012>, 07/01/ 2019.
- [5] Mukherjee A, Mukherjee V. Solution of optimal power flow with FACTS devices using a novel oppositional krill herd algorithm. *Int J Electr Power Energy Syst* 2016;78:700–14. <http://dx.doi.org/10.1016/j.ijepes.2015.12.001>, 06/01/ 2016.
- [6] Prasad D, Mukherjee V. A novel symbiotic organisms search algorithm for optimal power flow of power system with FACTS devices. *Eng Sci Technol Int J* 2016;19(1):79–89. <http://dx.doi.org/10.1016/j.jestch.2015.06.005>, 03/01/ 2016.
- [7] Mahdad B, Sairi K, Bouktir T. Optimal power flow for large-scale power system with shunt FACTS using efficient parallel GA. *Int J Electr Power Energy Syst* 2010;32(5):507–17. <http://dx.doi.org/10.1016/j.ijepes.2009.09.013>, 06/01/ 2010.
- [8] Sita H, Reddy PU, Kiranmayi R. Optimal location and sizing of UPFC for optimal power flow in a deregulated power system using a hybrid algorithm. *Int J Ambient Energy* 2019;1–7. <http://dx.doi.org/10.1080/01430750.2019.1707116>.
- [9] Aghaei J, Gitizadeh M, Kaji M. Placement and operation strategy of FACTS devices using optimal continuous power flow. *Sci Iran* 2012;19(6):1683–90. <http://dx.doi.org/10.1016/j.scient.2012.04.021>, 12/01/ 2012.
- [10] Ambriz-Pérez H, Acha E, Fuente-Esquivel CR. TCSC-firing angle model for optimal power flow solutions using Newton's method. *Int J Electr Power Energy Syst* 2006;28(2):77–85. <http://dx.doi.org/10.1016/j.ijepes.2005.10.003>, 02/01/ 2006.
- [11] Katebi J, Shoaeei-parchin M, Shariati M, Trung NT, Khorami M. Developed comparative analysis of metaheuristic optimization algorithms for optimal active control of structures. *Eng Comput* 2020;36(4):1539–58. <http://dx.doi.org/10.1007/s00366-019-00780-7>, 10/01 2020.
- [12] Oloyede M, Hancke G, Myburgh H, Onumanyi A. A new evaluation function for face image enhancement in unconstrained environments using metaheuristic algorithms. *EURASIP J Image Video Process* 2019;2019(1):27. <http://dx.doi.org/10.1186/s13640-019-0418-7>, 01/30 2019.
- [13] Ezugwu AE. Nature-inspired metaheuristic techniques for automatic clustering: a survey and performance study. *SN Appl Sci* 2020;2(2):273. <http://dx.doi.org/10.1007/s42452-020-2073-0>, 01/25 2020.
- [14] Nayeri S, Tavakoli M, Tanhaeean M, Jolai F. A robust fuzzy stochastic model for the responsive-resilient inventory-location problem: comparison of metaheuristic algorithms. *Ann Oper Res* 2021. <http://dx.doi.org/10.1007/s10479-021-03977-6>, 03/04 2021.
- [15] Halim AH, Ismail I, Das S. Performance assessment of the metaheuristic optimization algorithms: an exhaustive review. *Artif Intell Rev* 2021;54(3):2323–409. <http://dx.doi.org/10.1007/s10462-020-09906-6>.
- [16] Ezugwu AE, Adeleke OJ, Akinyelu AA, Viriri S. A conceptual comparison of several metaheuristic algorithms on continuous optimisation problems. *Neural Comput Appl* 2020;32(10):6207–51. <http://dx.doi.org/10.1007/s00521-019-04132-w>, 05/01 2020.
- [17] Bansal S. Performance comparison of five metaheuristic nature-inspired algorithms to find near-OGRs for WDM systems. *Artif Intell Rev* 2020;53(8):5589–635. <http://dx.doi.org/10.1007/s10462-020-09829-2>, 12/01 2020.
- [18] Vanchinathan K, Selvaganesan N. Adaptive fractional order PID controller tuning for brushless DC motor using artificial bee colony algorithm. *Results Control Optim* 2021;4:100032. <http://dx.doi.org/10.1016/j.rico.2021.100032>, 09/01/ 2021.
- [19] Zimmerman RD, Murillo-Sánchez CE, Thomas RJ. MATPOWER: Steady-state operations, planning, and analysis tools for power systems research and education. *IEEE Trans Power Syst* 2011;26(1):12–9.
- [20] Sulaiman MH, Mustafa Z, Saari MM, Daniyal H. Barnacles mating optimizer: A new bio-inspired algorithm for solving engineering optimization problems. *Eng Appl Artif Intell* 2020;87:103330. <http://dx.doi.org/10.1016/j.engappai.2019.103330>, 01/01/ 2020.
- [21] Sulaiman MH, et al. Barnacles mating optimizer: A bio-inspired algorithm for solving optimization problems. In: 2018 19th IEEE/ACIS international conference on software engineering, artificial intelligence, networking and parallel/distributed computing. 2018, p. 265–70. <http://dx.doi.org/10.1109/SNPDC.2018.8441097>, 27-29 2018.
- [22] Sulaiman MH, Mustafa Z, Saari MM, Daniyal H, Musirin I, Daud MR. Barnacles mating optimizer: An evolutionary algorithm for solving optimization. In: 2018 IEEE international conference on automatic control and intelligent systems. 2018, p. 99–104. <http://dx.doi.org/10.1109/12CACIS.2018.8603703>, 20-20 Oct. 2018.
- [23] Faramarzi A, Heidarinejad M, Mirjalili S, Gandomi AH. Marine predators algorithm: A nature-inspired metaheuristic. *Expert Syst Appl* 2020;152:113377. <http://dx.doi.org/10.1016/j.eswa.2020.113377>, 08/15/ 2020.
- [24] Mirjalili S. Moth-flame optimization algorithm: A novel nature-inspired heuristic paradigm. *Knowl-Based Syst* 2015;89:228–49. <http://dx.doi.org/10.1016/j.knosys.2015.07.006>, 11/01/ 2015.
- [25] Eberhart R, Kennedy J. A new optimizer using particle swarm theory. In: Proceedings of the sixth international symposium on micro machine and human science. MHS'95, 1995, p. 39–43. <http://dx.doi.org/10.1109/MHS.1995.494215>, 4-6 Oct. 1995.
- [26] Rashedi E, Nezamabadi-pour H, Saryzadi S. GSA: A gravitational search algorithm. *Inform Sci* 2009;179(13):2232–48. <http://dx.doi.org/10.1016/j.ins.2009.03.004>, 06/13/ 2009.
- [27] Rao RV, Savsani VJ, Vakharia DP. Teaching–learning-based optimization: A novel method for constrained mechanical design optimization problems. *Comput Aided Des* 2011;43(3):303–15. <http://dx.doi.org/10.1016/j.cad.2010.12.015>, 03/01/ 2011.
- [28] Rao RV, Savsani VJ, Vakharia DP. Teaching–learning-based optimization: An optimization method for continuous non-linear large scale problems. *Inform Sci* 2012;183(1):1–15. <http://dx.doi.org/10.1016/j.ins.2011.08.006>, 01/15/ 2012.
- [29] Črepinšek M, Liu S-H, Mernik L. A note on teaching–learning-based optimization algorithm. *Inform Sci* 2012;212:79–93. <http://dx.doi.org/10.1016/j.ins.2012.05.009>, 12/01/ 2012.
- [30] Waghmare G. Comments on a note on teaching–learning-based optimization algorithm. *Inform Sci* 2013;229:159–69. <http://dx.doi.org/10.1016/j.ins.2012.11.009>, 04/20/ 2013.
- [31] Labs S, S L. Teaching learning based optimization. SKS Labs; 2020. <https://www.mathworks.com/matlabcentral/fileexchange/65628-teaching-learning-based-optimization>. (Accessed 16 May 2020).
- [32] Boucekara HREH, Abido MA, Boucherma M. Optimal power flow using teaching-learning-based optimization technique. *Electr Power Syst Res* 2014;114:49–59. <http://dx.doi.org/10.1016/j.epsr.2014.03.032>, 09/01/ 2014.
- [33] Askari Q, Saeed M, Younas I. Heap-based optimizer inspired by corporate rank hierarchy for global optimization. *Expert Syst Appl* 2020;161:113702. <http://dx.doi.org/10.1016/j.eswa.2020.113702>, 12/15/ 2020.